



---

# Novel 2D Photonic Crystals Structures

**Christopher J. Summers,  
Curtis W. Neff and Tsuyoshi Yamashita**

**School of Materials Science and Engineering  
Georgia Institute of Technology  
Atlanta, Georgia 30332-0245  
[www.nanophotonics.gatech.edu](http://www.nanophotonics.gatech.edu)**

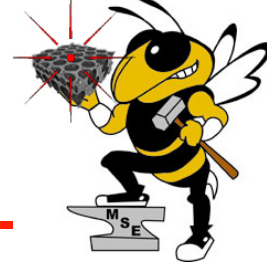
**First International Symposium on Optoelectronics  
in Optics Valley of China  
Wuhan, China  
2<sup>rd</sup> – 4<sup>th</sup> November, 2005**

# Photonic Crystal Programs Overview

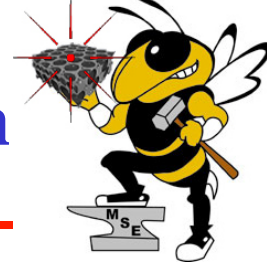
---



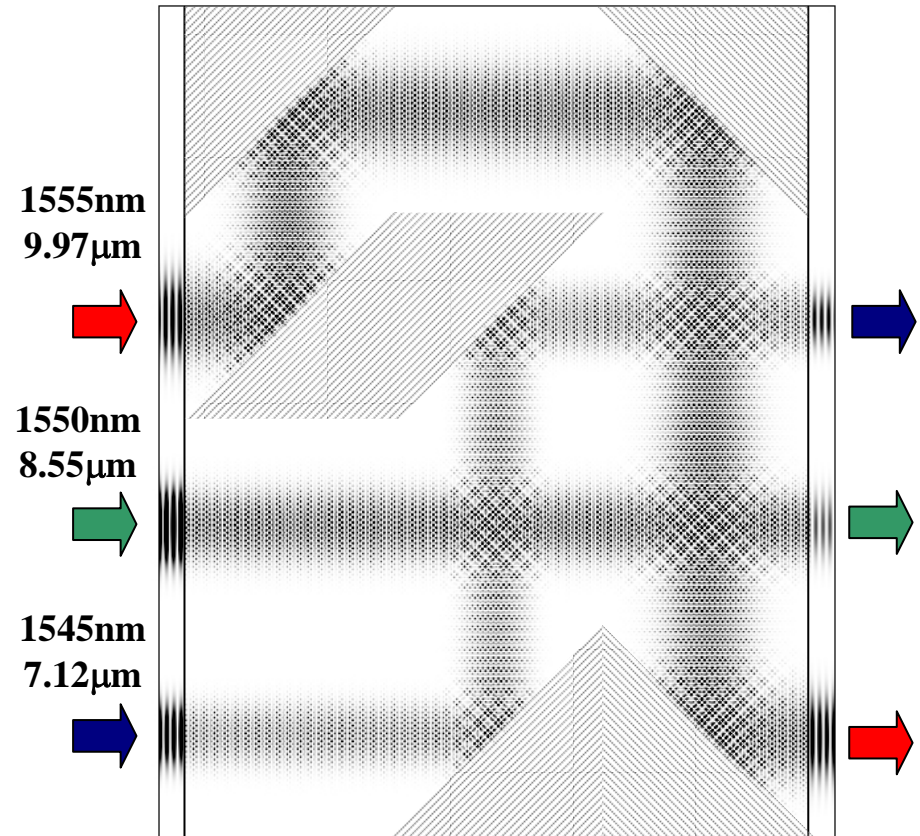
- **3D Photonic Crystal Structures**
  - PC Micro-cavities, Phosphors
  - Atomic Layer Epitaxy: Templating
  - Inverse/Non Close Packed Opals
  - Holographic Templates
- **2D Photonic Crystal Waveguides**
  - Triangular and Square lattices
  - Superlattices – triangular based
  - Non-Linear Structures



- **2D Photonic Crystal Structures**
  - **“Virtual Waveguides”** Low divergent propagation in slab waveguides
  - **“Fabry-Perot Etalons”** – spectral tuning
- **2D Superlattice Photonic Crystal Waveguide Structures**
  - Superlattices – triangular based
  - Static; Hybrid; E/O superlattice
  - Non-Linear Structures
    - Liquid Crystal Infiltration of 2D PC
    - Non-linear & Electro-Optical (EO) materials
- **Impact of New Structures & Materials**
  - Tunable effects



- **Advantages of free-space optics**
  - No coupling
  - Intersections allowed
  - Broadband operation
- **Advantages of integrated optics**
  - Confined beams
  - No hermetic packaging
  - One lithography step
- **Disadvantages**
  - Small feature sizes required (beam size  $\sim 15a$ )
  - Compared to 2-3a for line defect PC waveguides
- **PC mirrors have lower PBG**



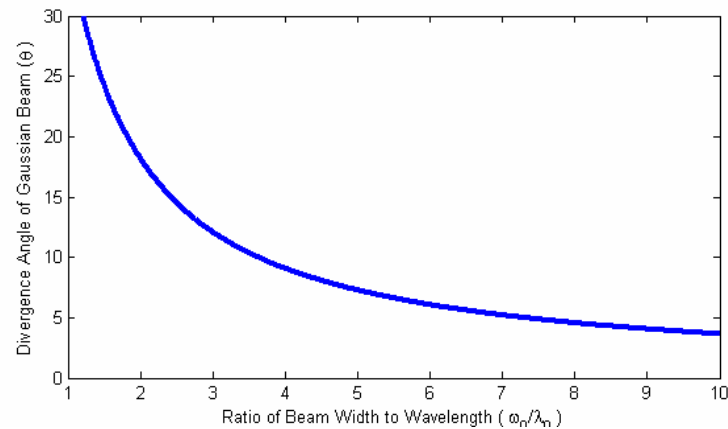
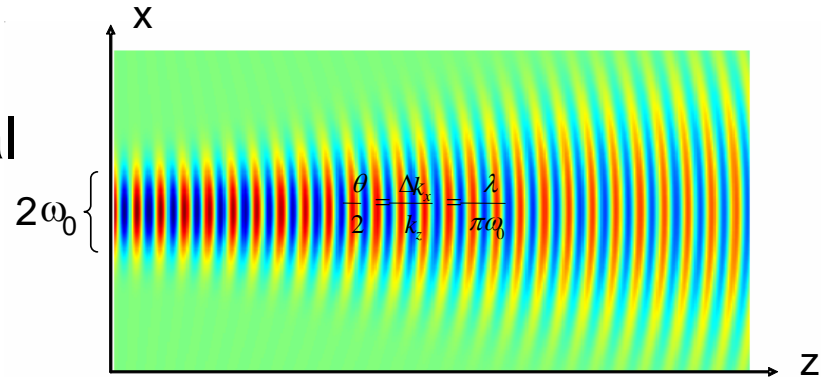
- Collimation exploits same phenomena as sub-wavelength focusing



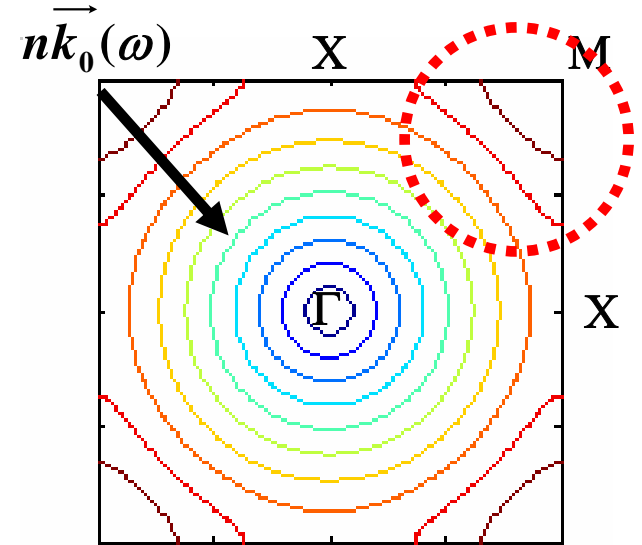
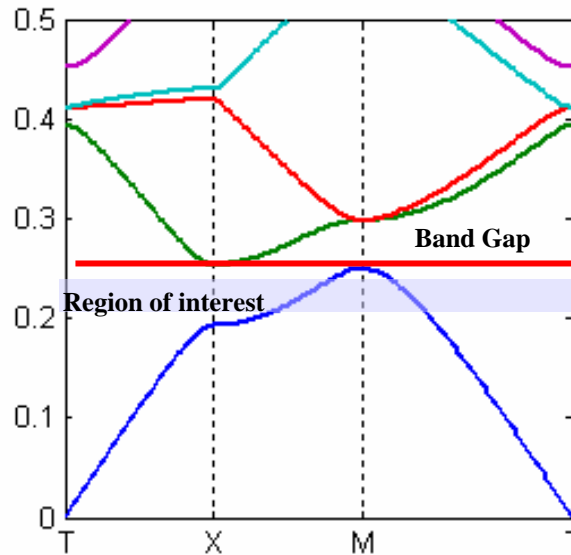
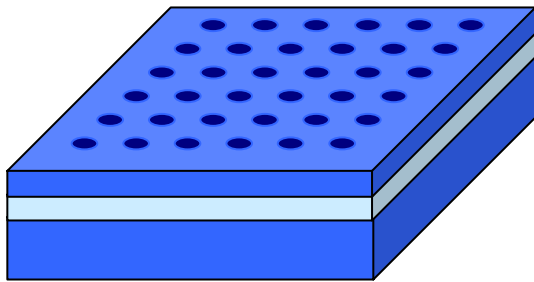
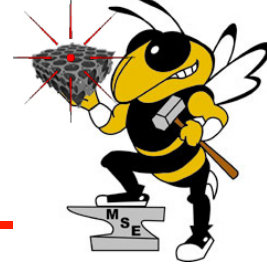
- A Gaussian beam spreads in the paraxial approximation in an isotropic material as:

$$\frac{\theta}{2} = \frac{\Delta k_x}{k_z} = \frac{\lambda}{\pi \omega_0}$$

- The divergence determines the coupling efficiency into the photonic crystal



# Analysis of 2D Photonic Crystals Square Lattice



- Square lattice
  - Hole diameter
  - Refractive index

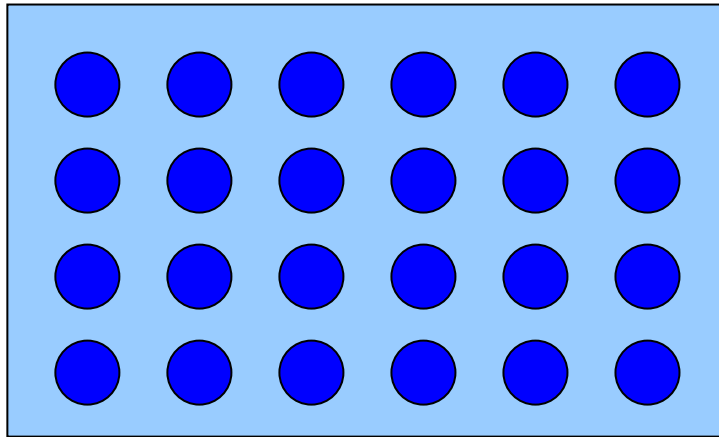
- Band Diagram
  - Boundaries of the band surface
  - Identification of band gaps

- Allowed Wave Vector Curve
  - Equifrequency curves of the band surface
  - Identification of propagation effects

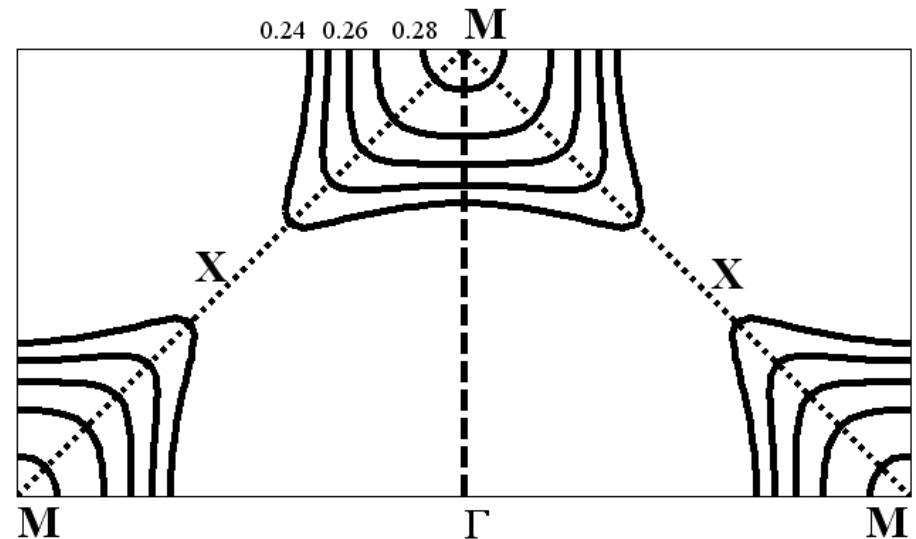
# Concavity Reversal Near Brillouin Zone Boundaries



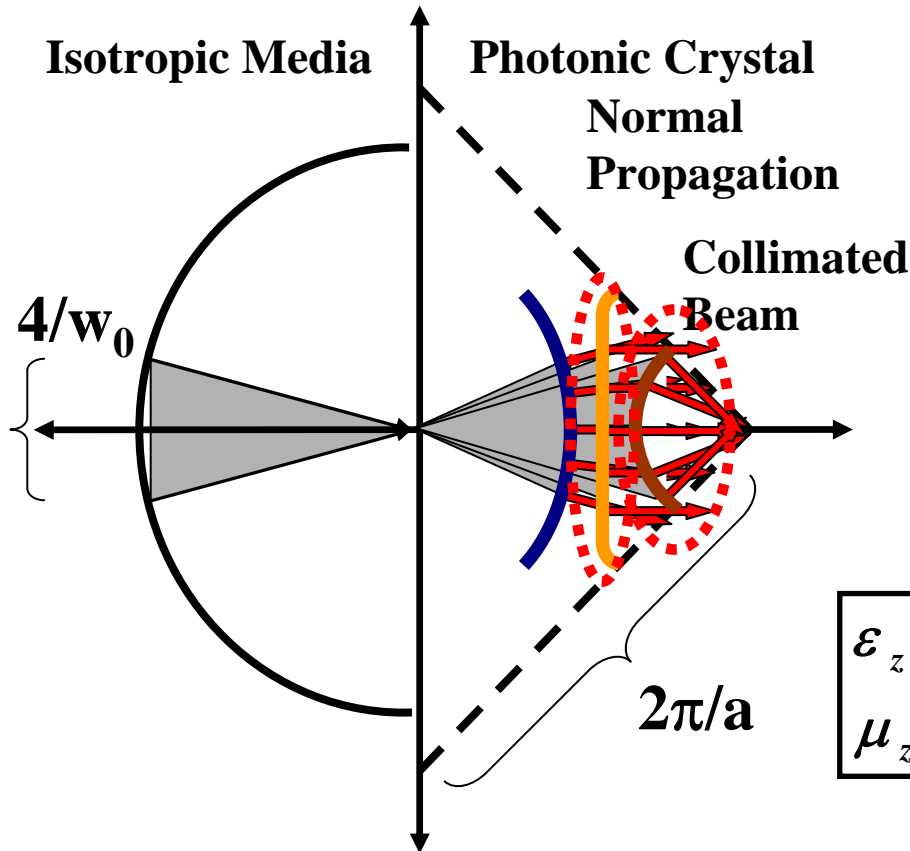
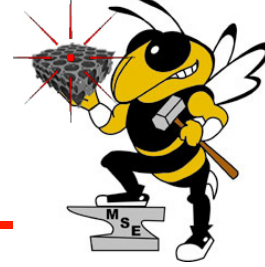
- First band concavity reverses near the M point in a square lattice
- Dispersion curve approximately linear and normal to the  $\Gamma$ -M direction near the concavity reversal
- Robust to small fluctuations in  $\lambda$  and  $r$
- Provides orthogonal grid of propagation for ease of design
- First band guarantees confinement along the thickness of the waveguide



$$r=0.2a, \epsilon_{\text{matrix}}=2, \epsilon_{\text{pillars}}=11$$



# Dispersion Curve Analysis of Square Lattice PC



- PC lattice designed to produce dispersion contours with a wide range of curvatures
  - Concave – normal propagation -- defocusing
  - Straight – collimated beam guiding
  - Convex – negative index for sub-wavelength focusing

**Negative Index Effect**

$\epsilon_z = \infty$	$\epsilon_z = \textit{negative}$
$\mu_z = \infty$	$\mu_z = \textit{negative}$

- **Canceling of Z-component leads to self-collimation**
- **Effective negative index for the energy propagation obtained**





# Self-Collimated Beams in FDTD Simulation

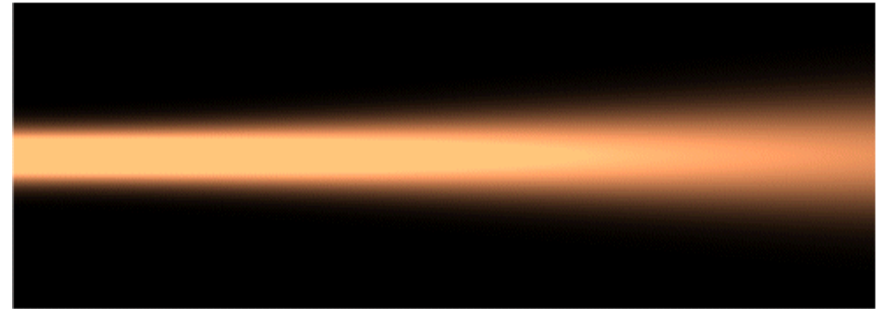


- FDTD simulation of self-collimation

- $\omega_n = 0.26$
- $\lambda = 1.55\text{mm}$

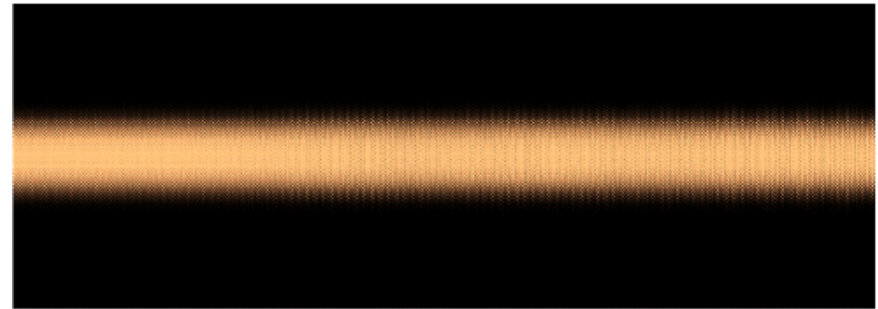
- Clear intensity confinement in photonic crystal

- ~25x longer propagation possible than in air
- No discernable beam spread for 120 $\mu\text{m}$  of propagation of a 8.5 $\mu\text{m}$  wide beam



Air

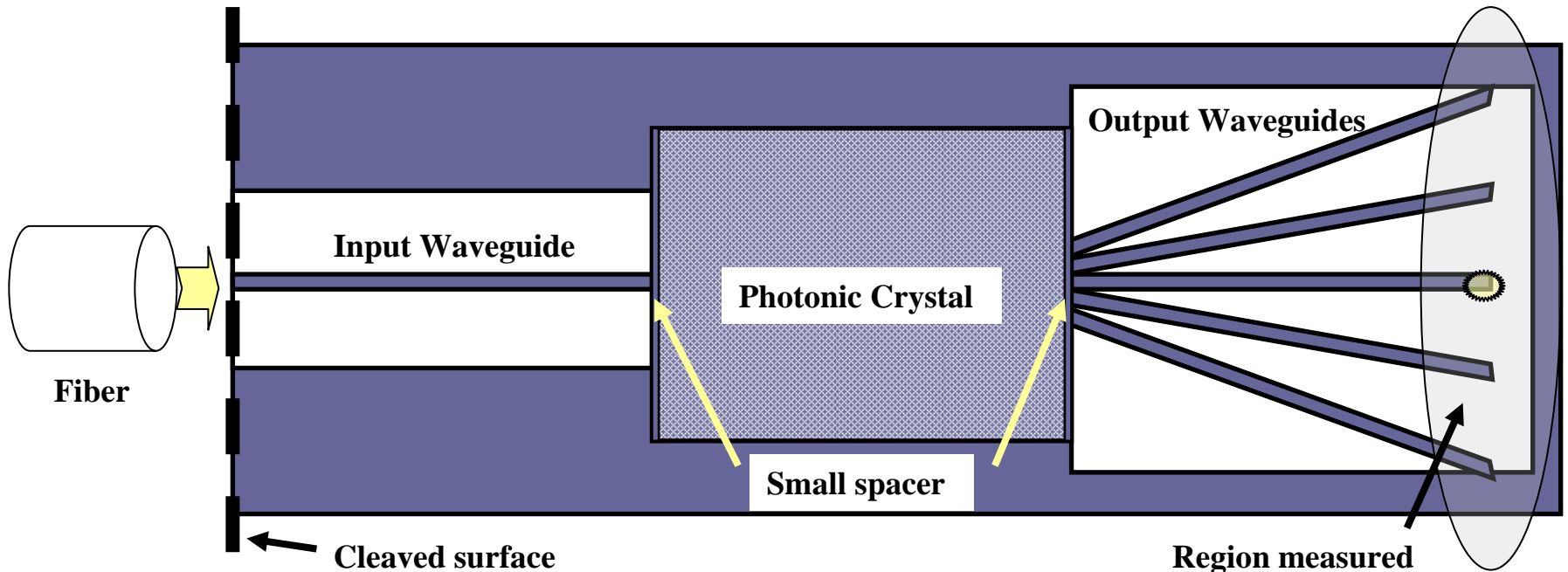
- Beam spread decreased by an order of magnitude or more with beam sizes as small as 5-10  $\lambda_0$



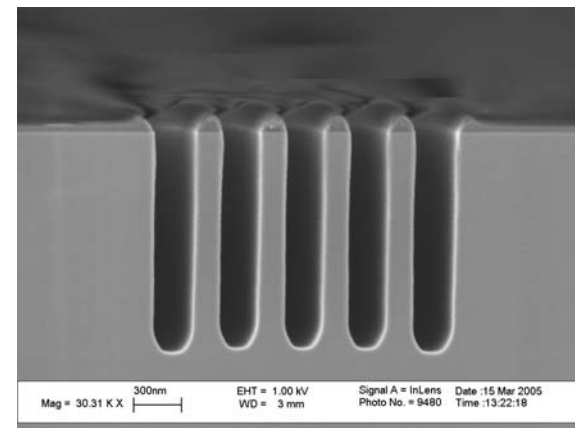
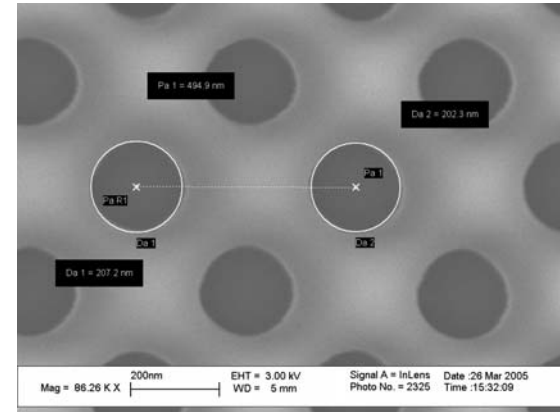
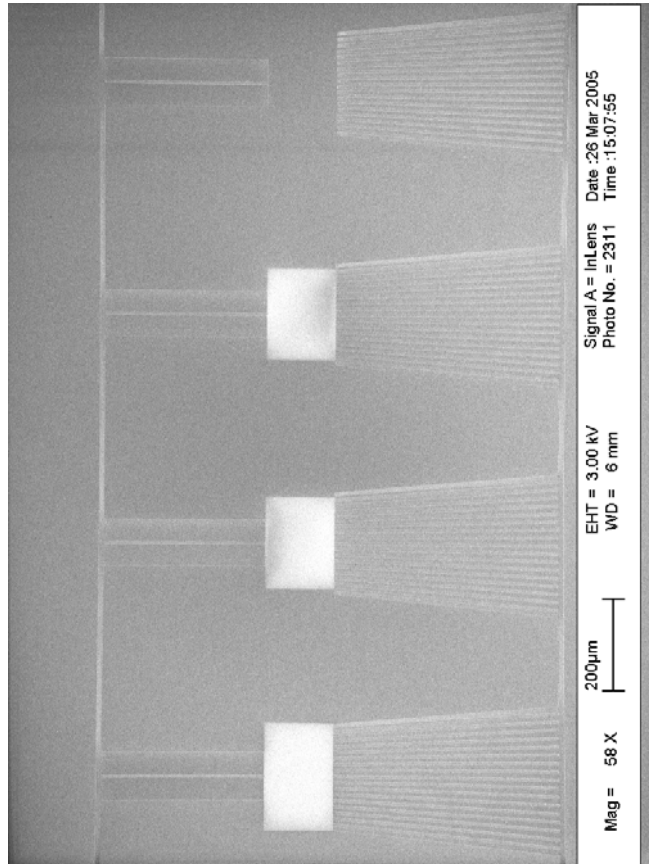
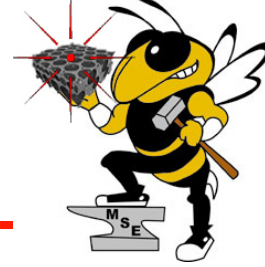
Photonic Crystal

- Applications include:

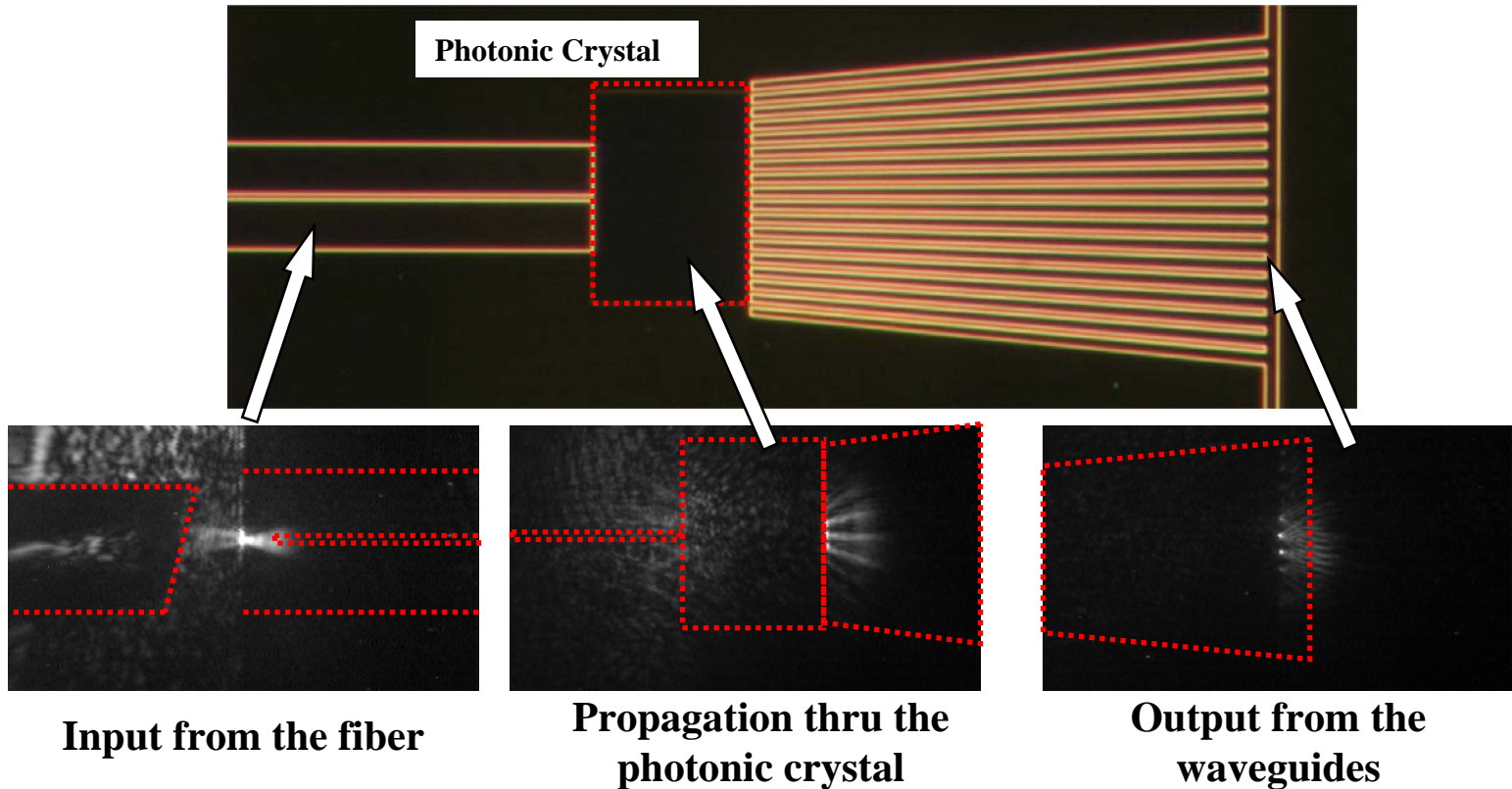
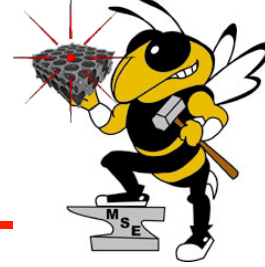
- Virtual waveguide interconnect system
- Miniaturization of conventional optical components for small beams



- Principle of operation
  - Gaussian like input from input waveguide
  - Beam spread observable from number of lit output waveguides
- Quality requirement
  - Smooth surfaces ( $<L_s/20$ )
  - Anisotropic sidewalls ( $<5^\circ$ )
  - Uniform hole sizes in photonic crystal ( $<5\%$  locally)
  - Large area  $\sim 150 \mu\text{m}^2$



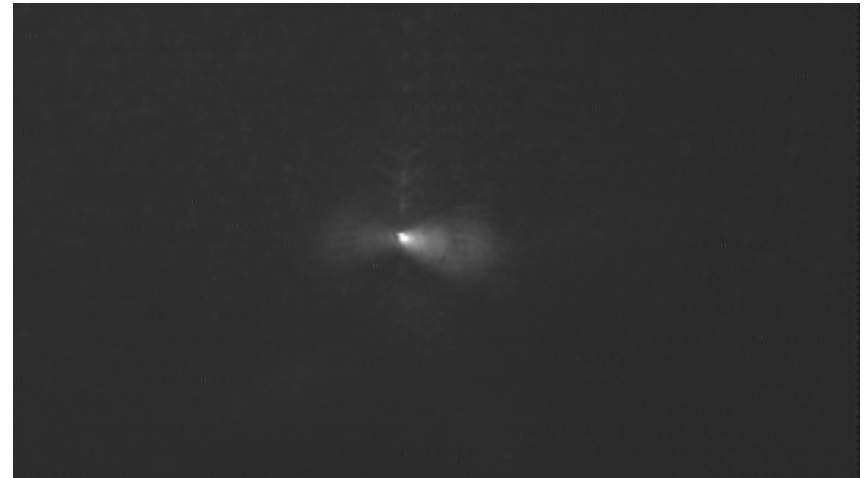
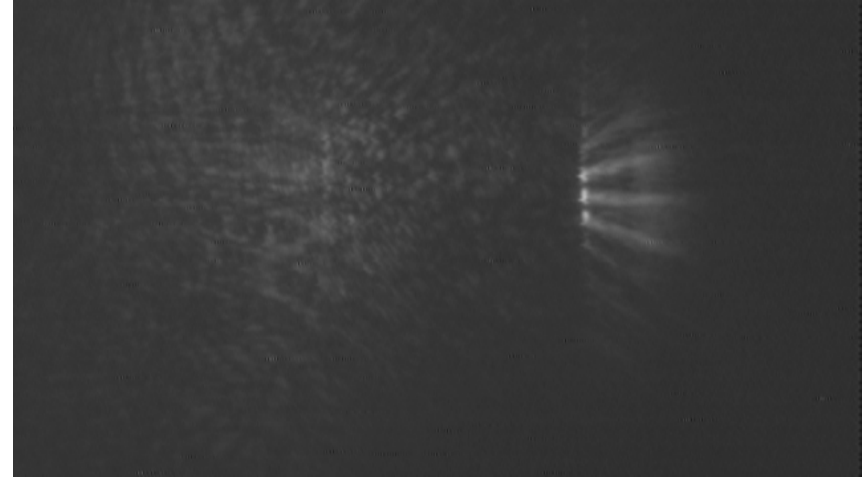
- Input waveguide, photonic crystal, fan of waveguides for analysis
- Examples of photonic crystal fabrication.



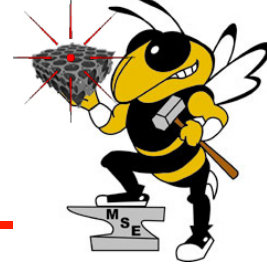
- Infrared camera utilized to view scattered light from the device



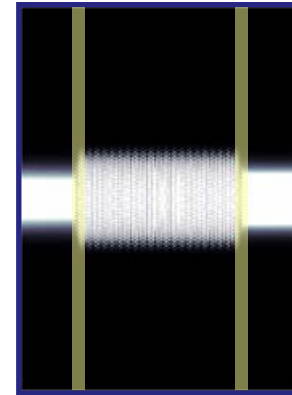
- Test structure with no photonic crystal:
  - Approximately 8 WGs lit up
  
- Test structure with “virtual waveguide” photonic crystal:
  - Only central waveguide lit up
  
- Very good beam collimation in PC



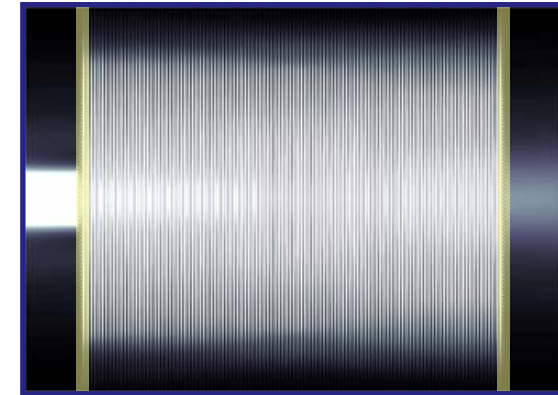
# Applications: Fabry-Perot Interferometer



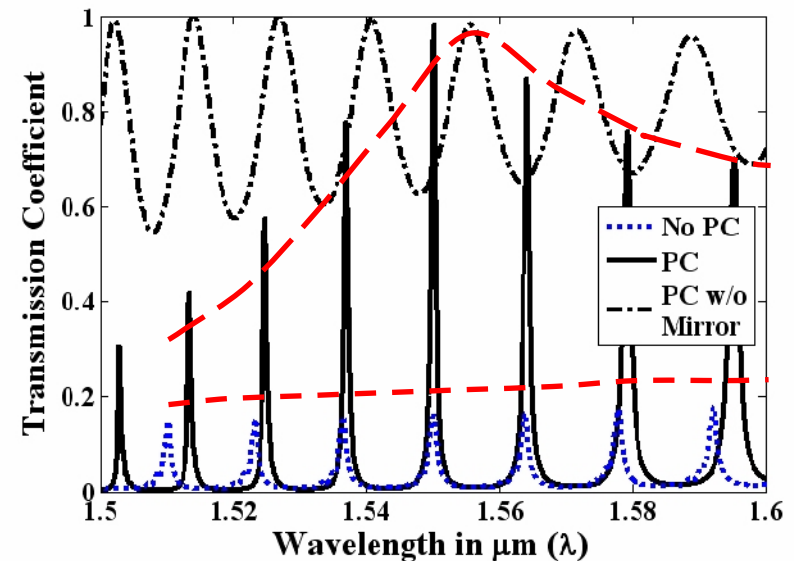
- Beam spread degrades performance
  - Beam size
  - Intensity leaks backward (<16% center intensity)
- Photonic crystal confines beam
  - >98% transmitted center intensity for mode near self-collimation
  - Can control bandwidth for selecting number and intensity of transmitted beams
- Concept extends to other interferometers and bulk optical devices



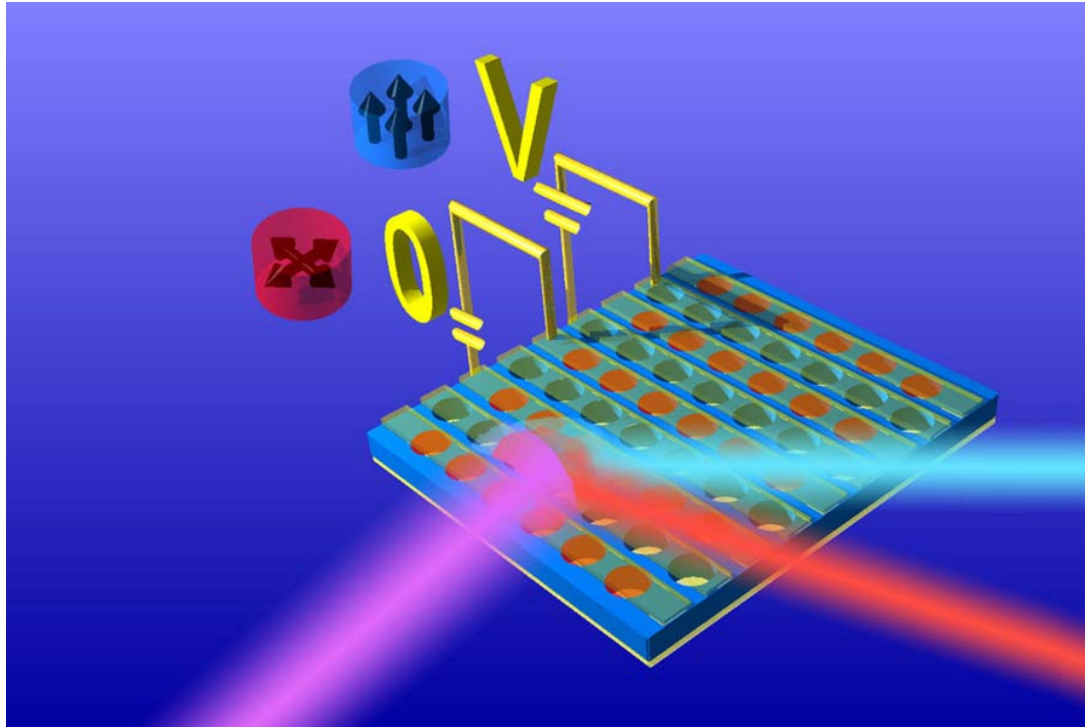
Photonic crystal



No photonic crystal



Transmitted intensity at center of beam



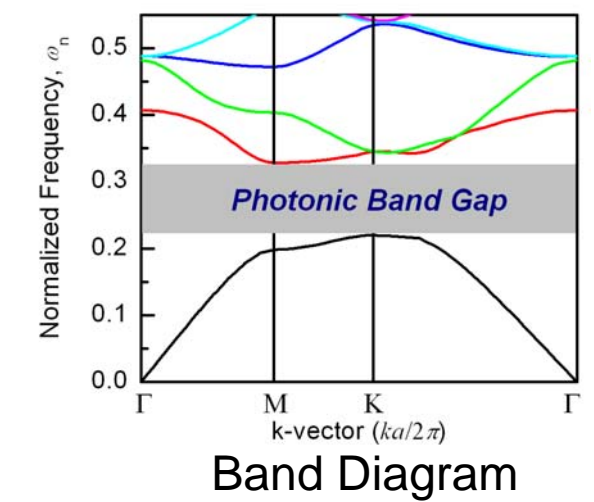
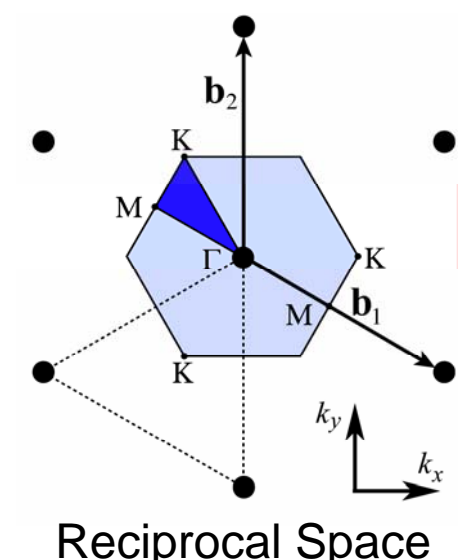
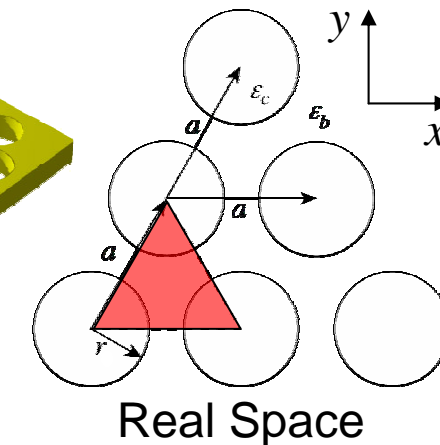
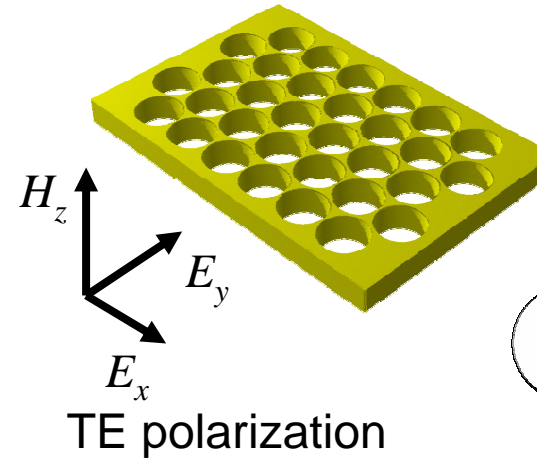
- Giant refraction
- Superprism
- Tunable refraction

# Two Dimensional PC: Triangular Lattice

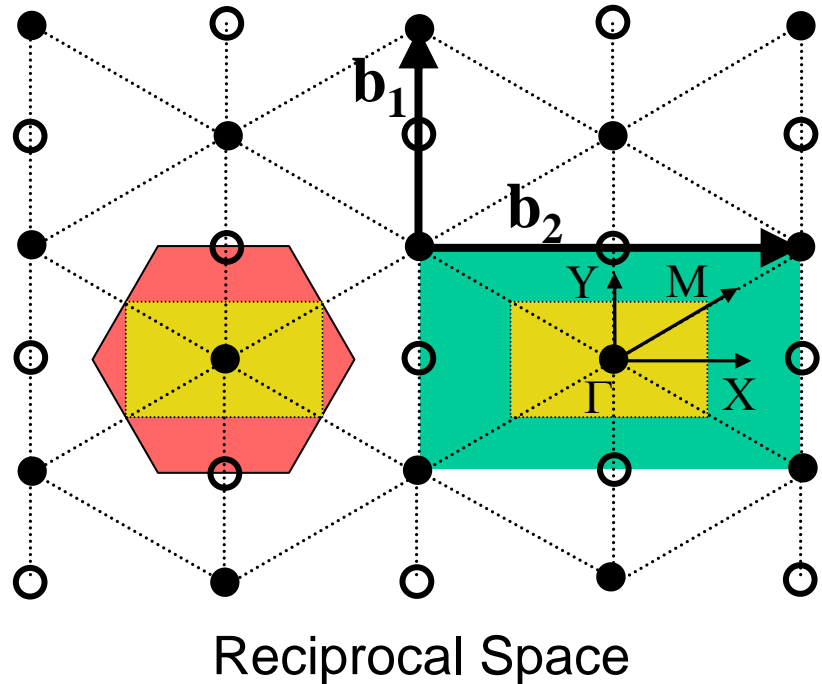
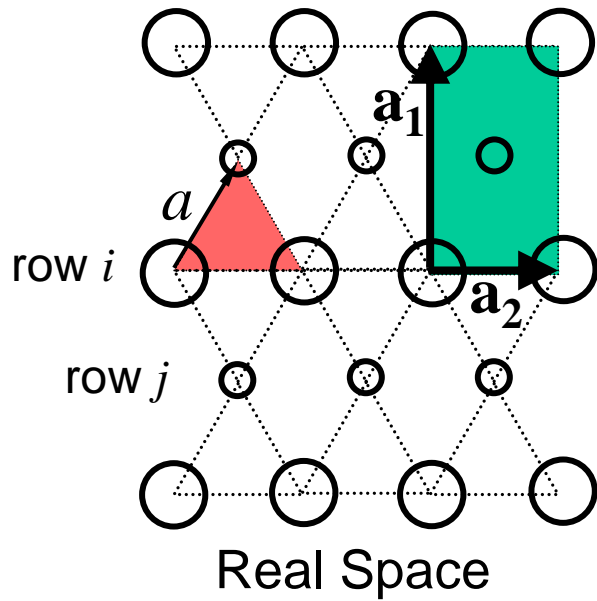
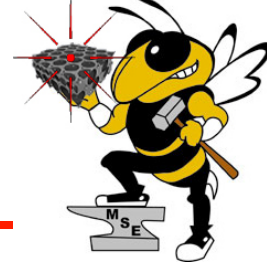


- Simpler structure than 3D
- Top-down fabrication
- Integration with planar circuits
- Simpler analysis of optical properties than 3D
- Can have full PBG (light in plane of PC)
- Giant refraction effects
- *Superprism* effects

- Band diagram: Plot of dispersion relationship,  $\omega(k)$ , along irreducible BZ boundary





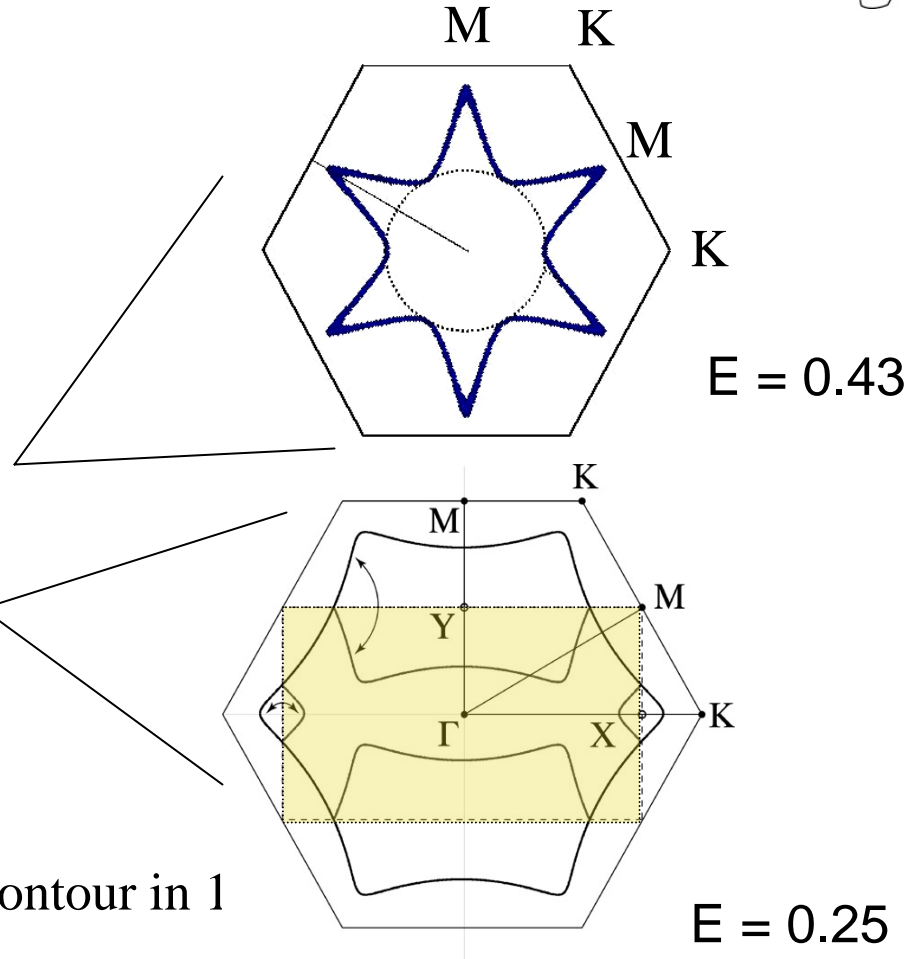
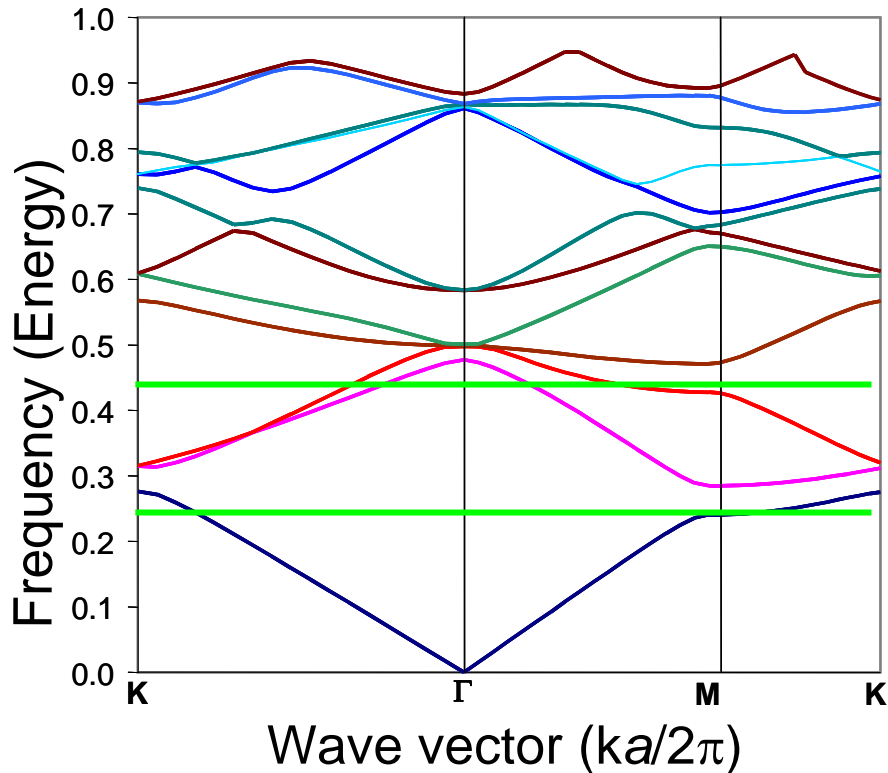


- Alternating rows possess different property ( $\Delta r$ ,  $\Delta n$ , or both)
- Unit cell definition with two holes per lattice point

- New BZ representation: hexagonal becomes rectangular
- BZ folding
- Symmetry reduction: six-fold to two-fold



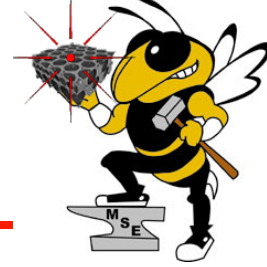
ZnS/Air Triangular Lattice



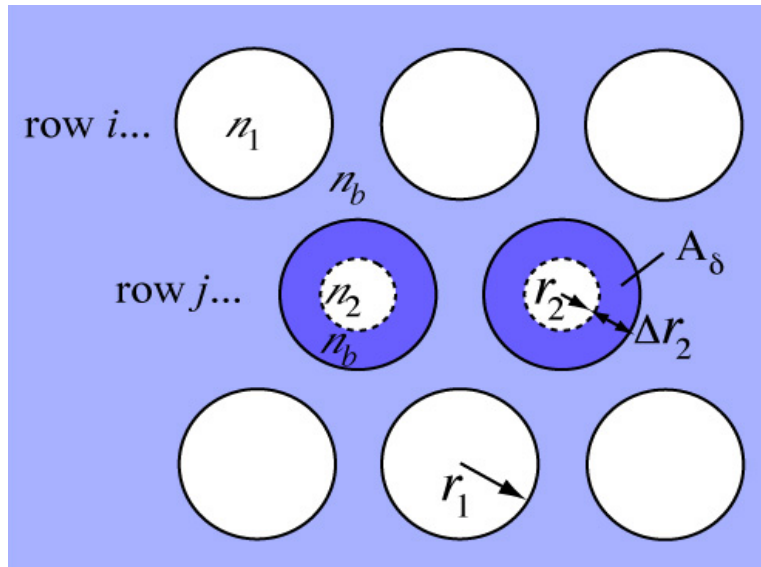
- Dispersion diagram: constant energy contour in 1
- Homogeneous medium  $\rightarrow$  circle
- Photonic crystal  $\rightarrow$  complex in shape
- Propagation of light normal to the dispersion curve, in direction of energy flow

# Static Superlattice Photonic Crystal

## Superlattice Strength: $r_2/r_1$



- Superlattice: hole radii,  $r_1$  &  $r_2$ , in adjacent rows  $[i, j]$ , respectively, Lattice vector  $a$
- Increasing superlattice strength accomplished by increasing  $\Delta n$  or  $\Delta r$  between rows



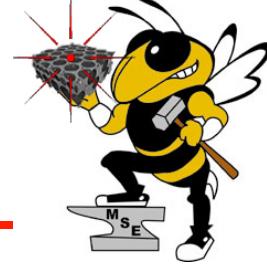
- Strength of superlattice defined as:  
extra dielectric added when  $r_2$  made smaller,  $r_2/r_1$  ratio

$$n_{eff} = \frac{n_b A_\delta + n_2 A_2}{A_1}$$

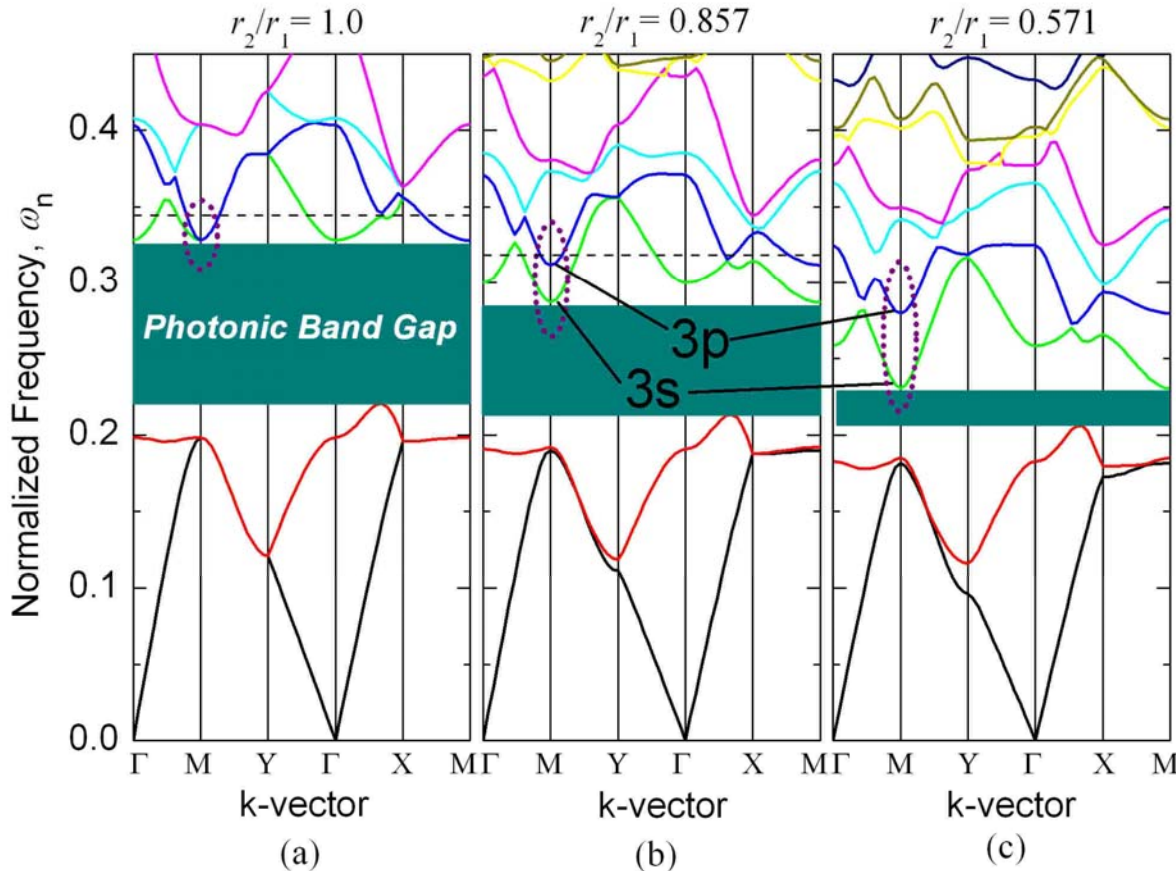
$$= n_b \left( 1 - \left( \frac{r_2}{r_1} \right)^2 \right) + n_2 \left( \frac{r_2}{r_1} \right)^2$$

- In Si, for  $r_2/r_1=0.857$ ,  $n_{eff}=1.654$  which is  $\Delta n=0.654$  between rows of holes
- To increase the strength of the superlattice. The radius of the columns of row  $j$  is decreased down to  $\Delta r_2=0.15a$  while  $r_1$  is kept constant

# Effect of SL Strength ( $r_2/r_1$ ) on Band Structure ( $\Delta r$ )

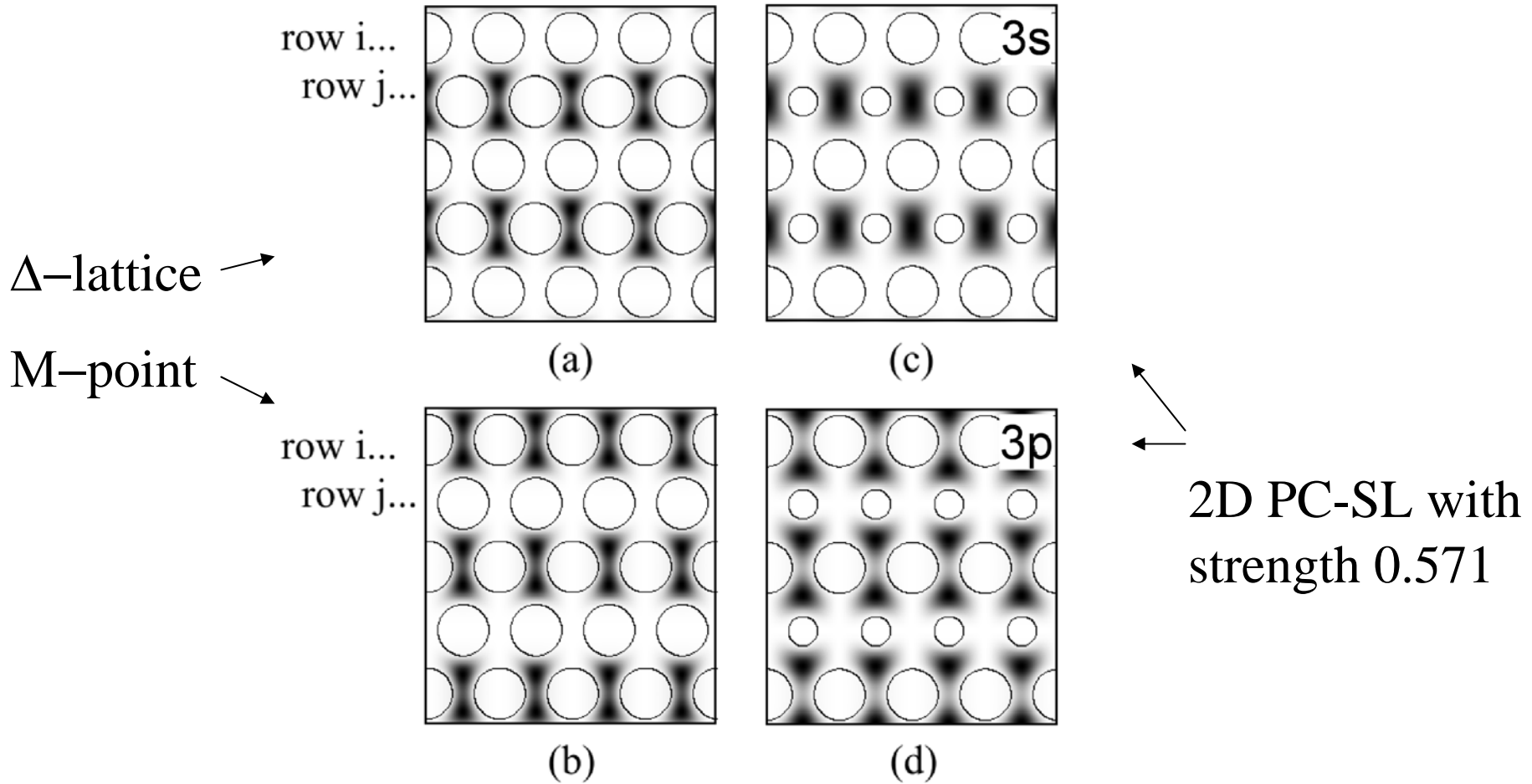


TE polarization



- Decreasing  $r_2$  increases dielectric material in structure
- Stronger effect on air bands than dielectric bands
- Shifts bands to lower frequencies
- Decreases width of PBG
- Increases band splitting
- Similar effect in dynamic superlattice when changing  $\Delta n$

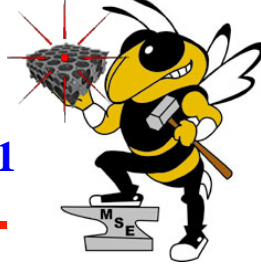
- Evolution of a static superlattice band structure with radius ratio  
(a)  $r_2/r_1 = 1$ , (b)  $r_2/r_1 = 0.857$ , (c)  $r_2/r_1 = 0.571$



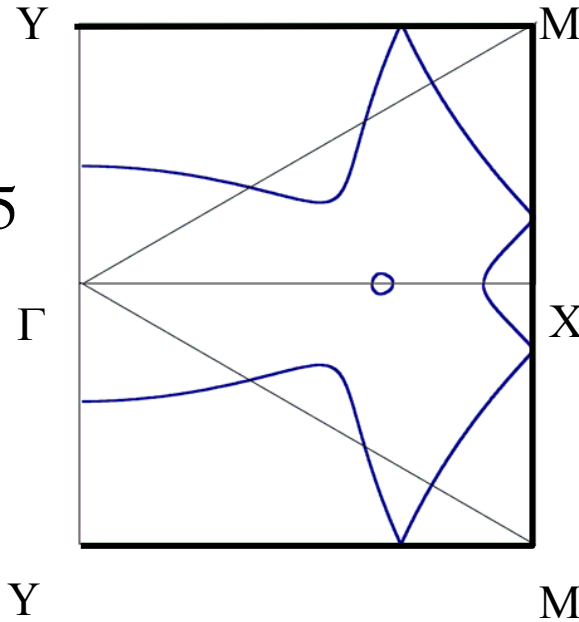
- a & b --- Degenerate states at bottom of air band at M-point  $\Delta$ -lattice
- c & d --- 3s and 3p states of the 2D PC-SL with strength 0.571



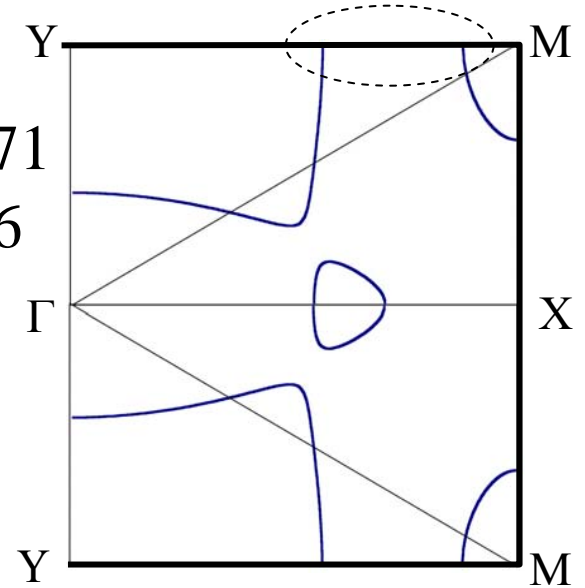
# Dispersion Contours: Dependence on $r_2/r_1$



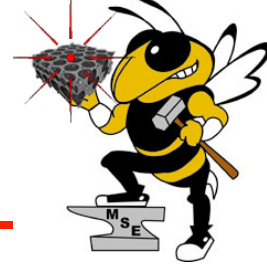
$r_2/r_1=1.0$   
 $\omega_n=0.435$



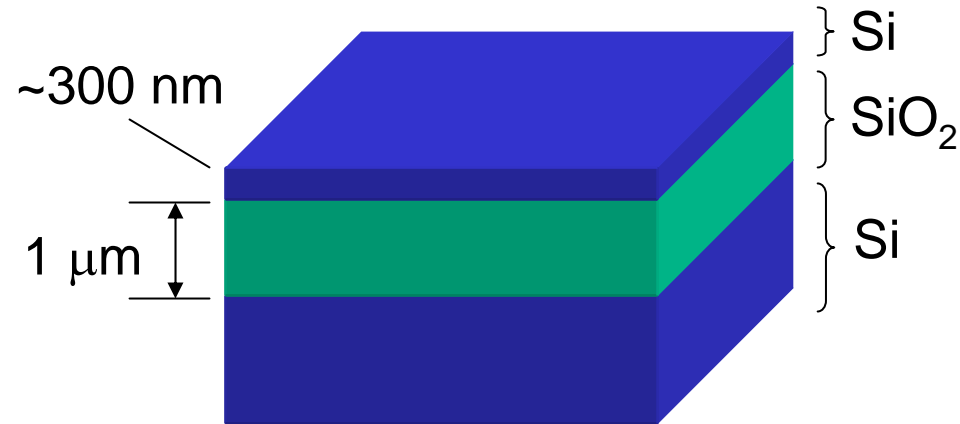
$r_2/r_1=0.571$   
 $\omega_n=0.366$



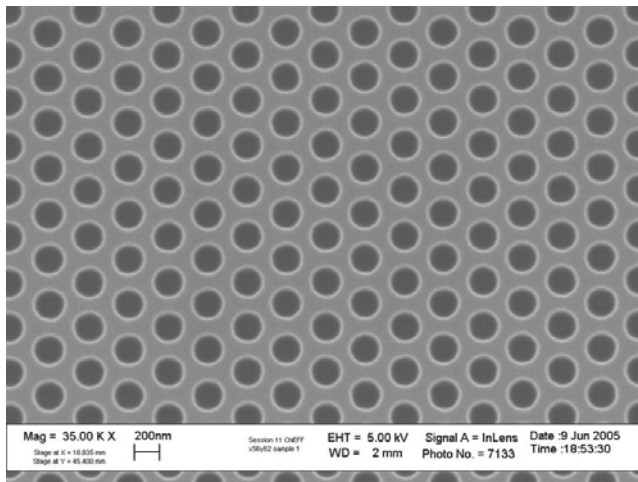
- For  $\Delta r = 0$ , ( $r_2/r_1=1$ ), BZ folding scheme straight forward: curves converge to a single point at BZ boundaries.
- Radius modulation ( $r_2/r_1 < 1$ ): curves diverge/repel at BZ boundaries
- Net result: relatively flat curvature in center of BZ with high curvature near BZ boundaries



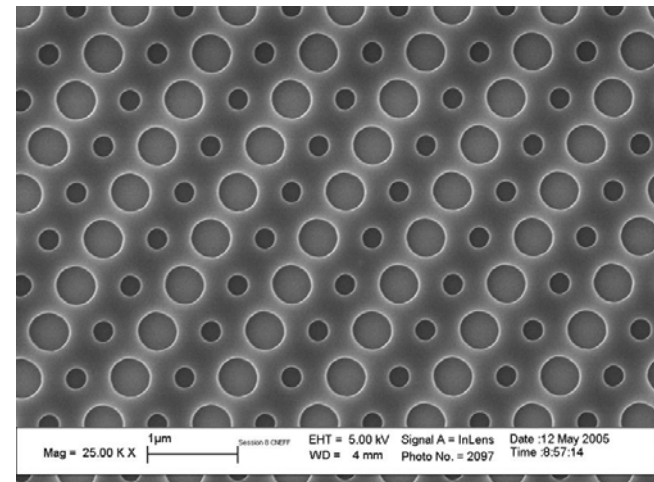
- E-beam lithography
- ICP dry etching with Chlorine/ $C_4F_6$  recipe
- $1 \text{ mm}^2$  area written using smaller unit patterns
- Lattice constant:  $a=358 \text{ nm}$
- Silicon slab waveguide (SWG)

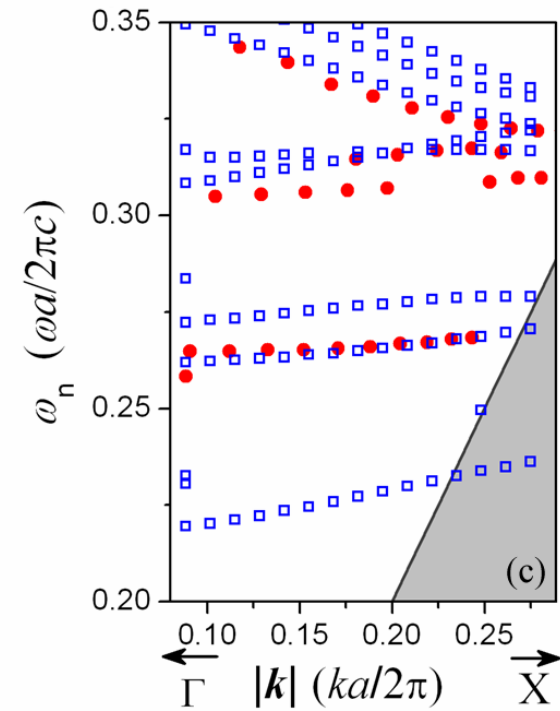
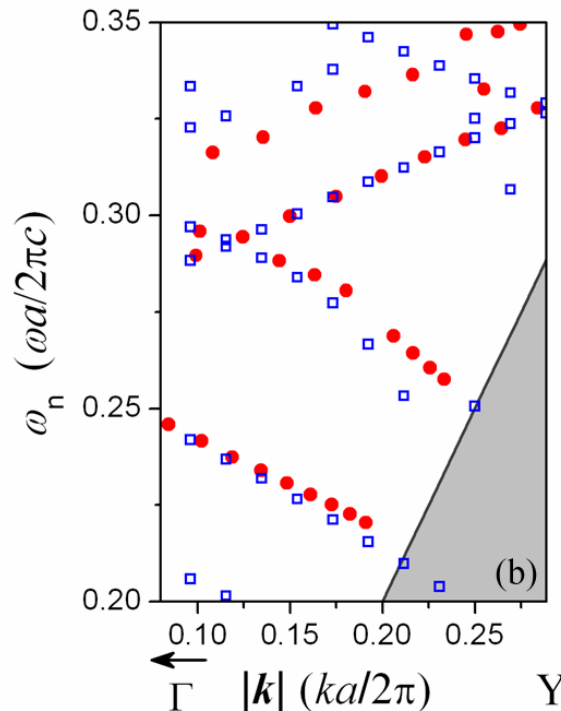
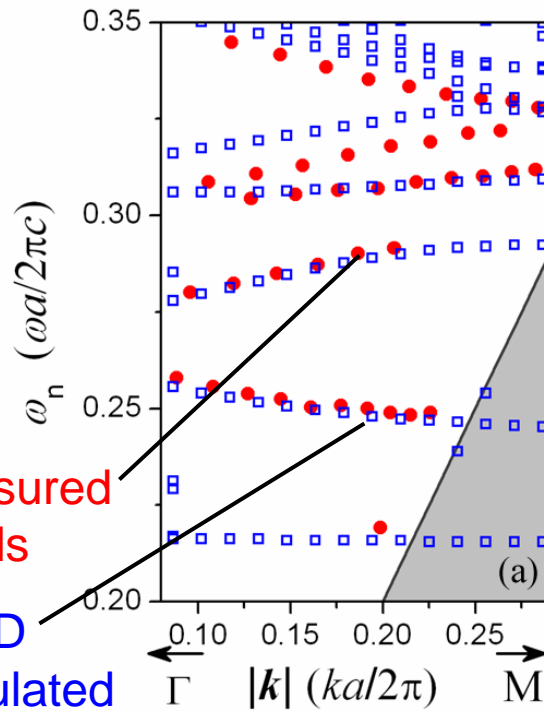


## Triangular Lattice



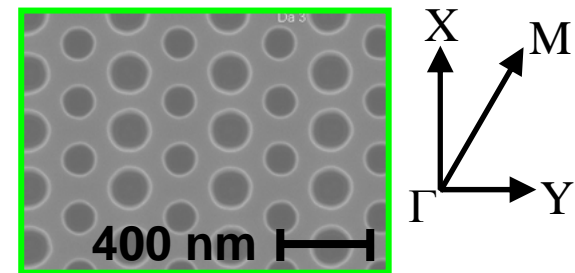
## SL Lattice



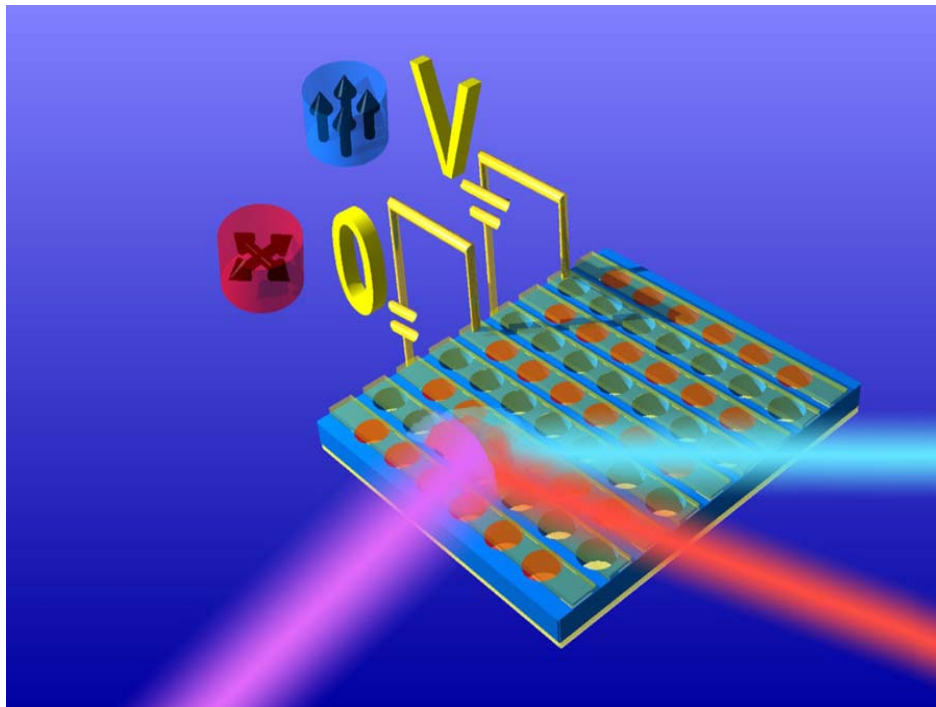
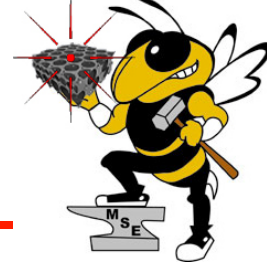


Measured bands  
FDTD calculated bands

- Dips in spectrum filtered and plotted as  $\omega$  vs.  $k$
- Full 3D FDTD calculations to match structure

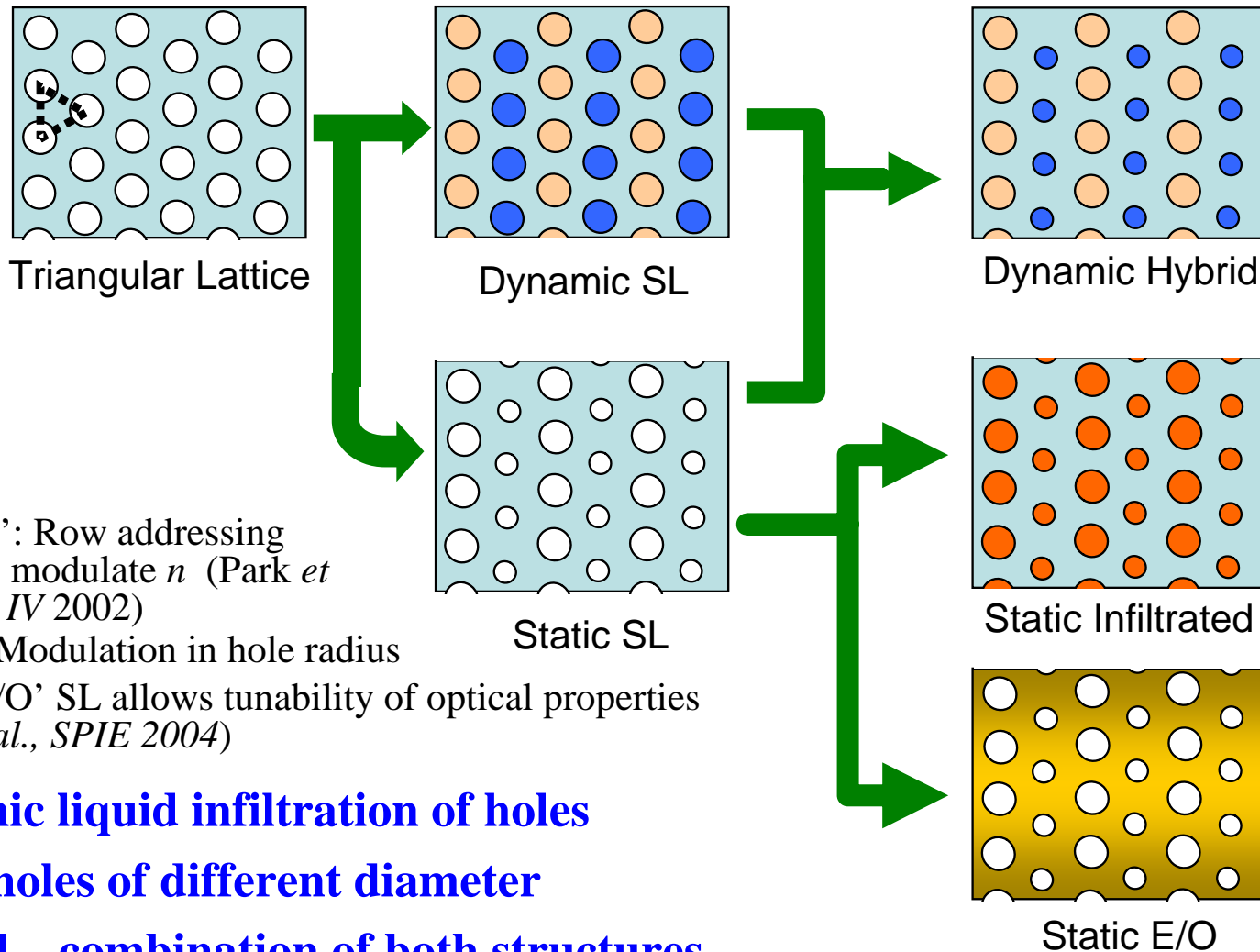






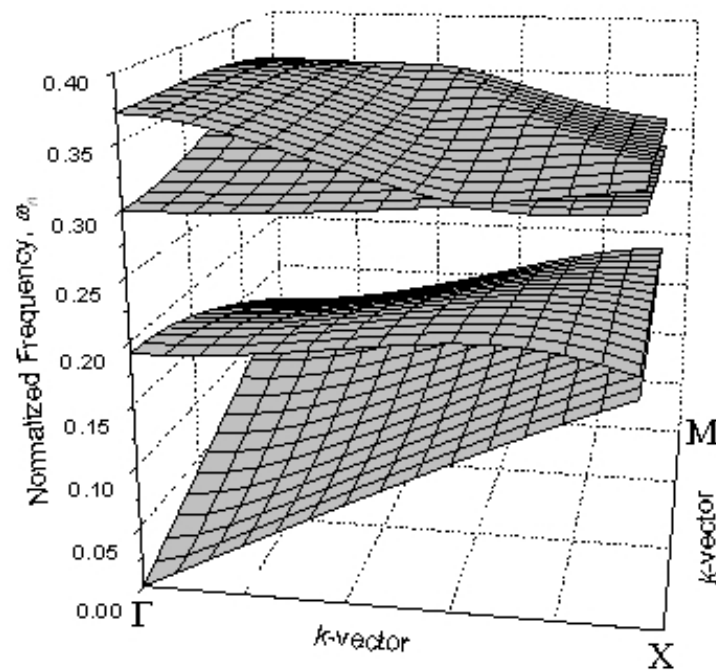
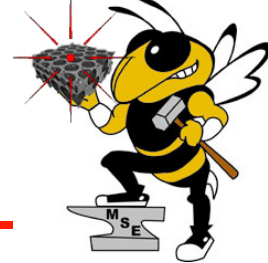
- **Concept:**
  - Dynamically change lattice property, i.e. refractive index, while under excitation
- **Consequences:**
  - Active beam steering
  - Tunable filtering
  - Signal modulation

# Superlattice Photonic Crystal Structures Based on Triangular Lattice



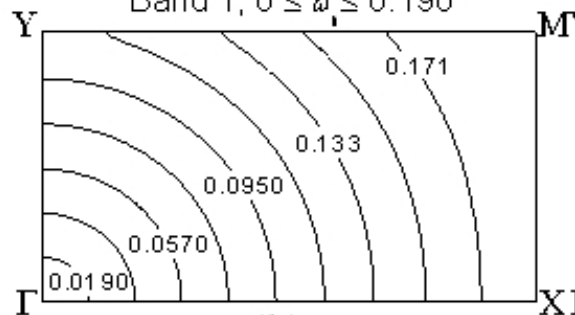
- ‘Dynamic’: Row addressing scheme to modulate  $n$  (Park *et al.*, *PECS IV* 2002)
- ‘Static’: Modulation in hole radius
- ‘Static E/O’ SL allows tunability of optical properties (Neff *et al.*, *SPIE* 2004)
- **Dynamic liquid infiltration of holes**
- **Static holes of different diameter**
- **Hybrid – combination of both structures**

# Dispersion Surfaces for First Four Bands of SSL Structures



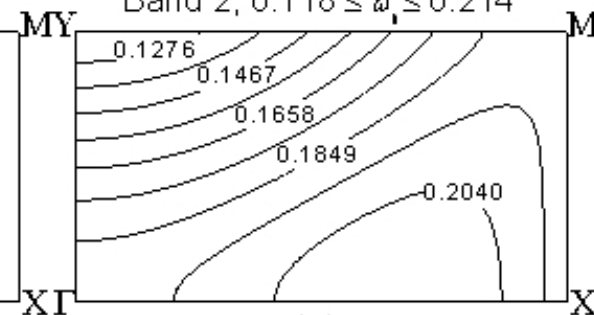
(a)

Band 1,  $0 \leq \omega_1 \leq 0.190$



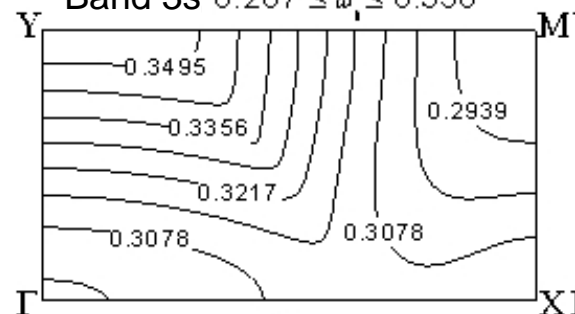
(b)

Band 2,  $0.118 \leq \omega_2 \leq 0.214$



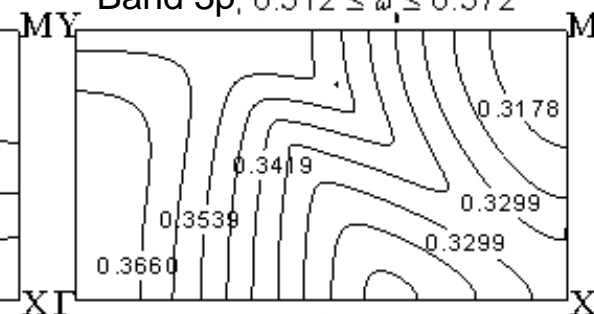
(c)

Band 3s,  $0.287 \leq \omega_3 \leq 0.356$

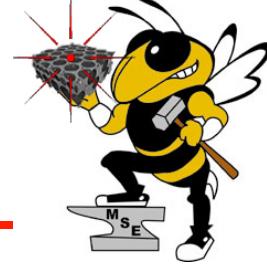


(d)

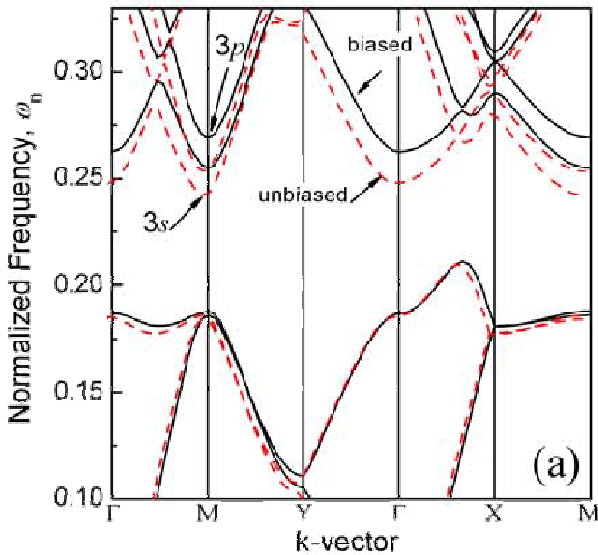
Band 3p,  $0.312 \leq \omega_3 \leq 0.372$



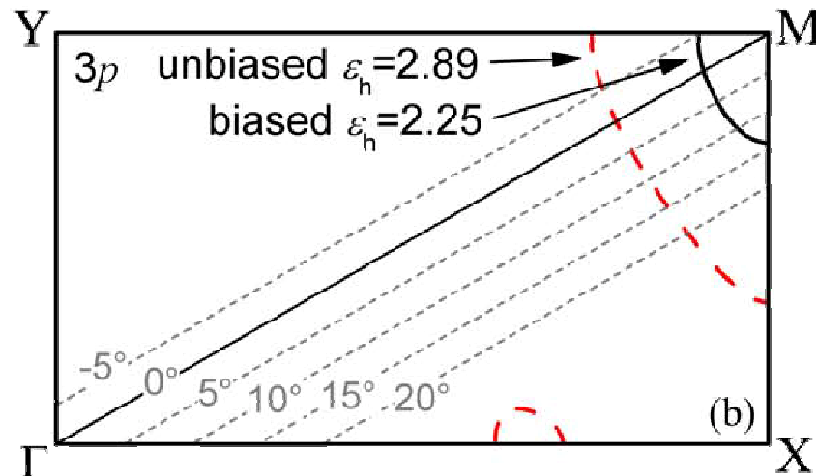
(e)



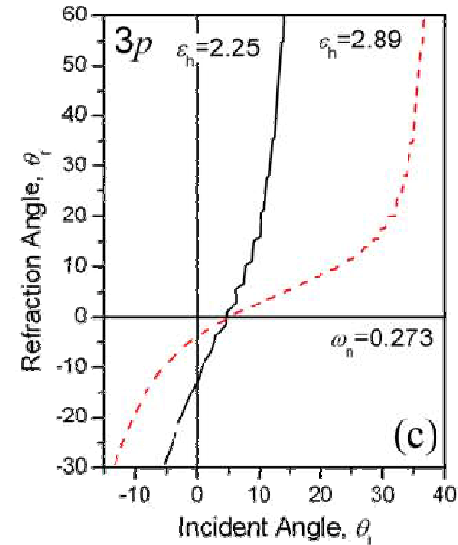
Band Structure



Dispersion Contours

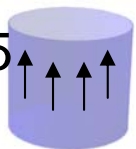


Refraction

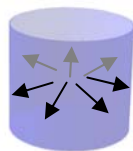


Biased

$\epsilon = 2.25$



Unbiased  
 $\epsilon = 2.89$



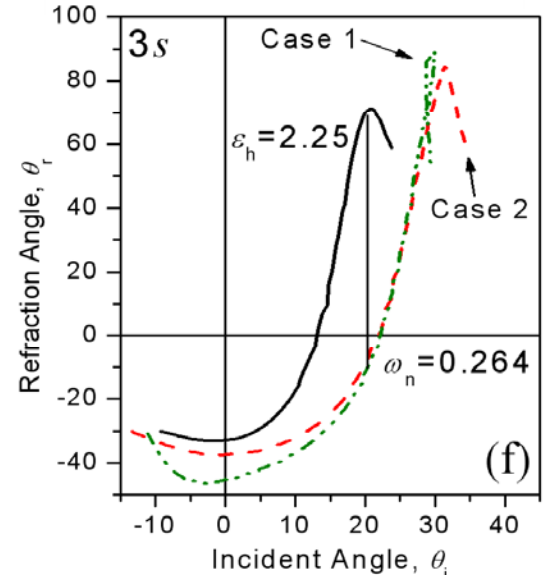
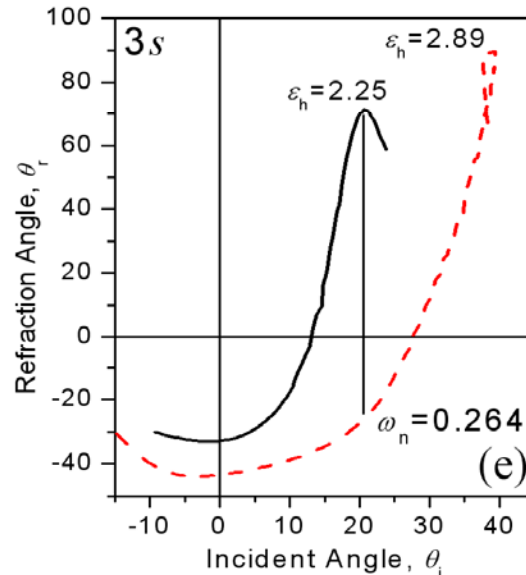
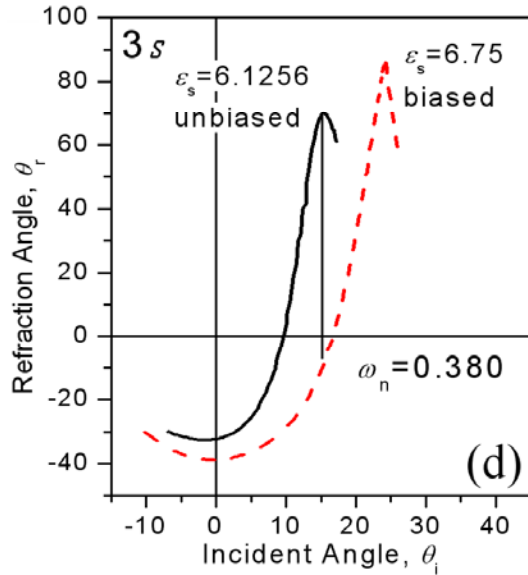
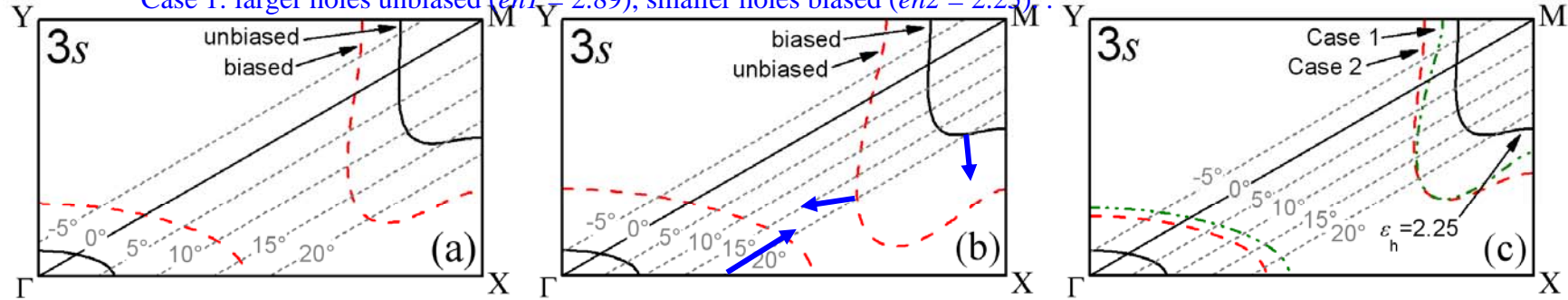
- Changing bias/unbias state changes alignment of LC director  $\rightarrow$  changes  $\epsilon$ 
  - Changes band structure
  - Changes dispersion contours
  - Changes refraction response

# Dispersion Contours and Refraction for Three SSL Devices -3s Band



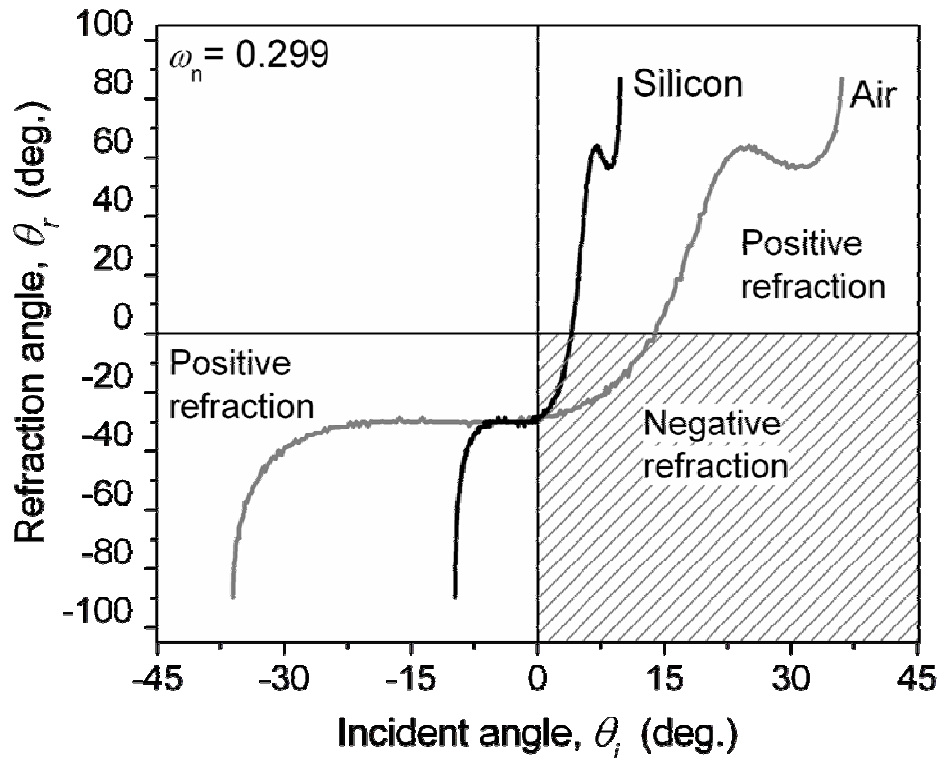
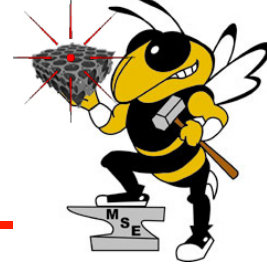
- (a & d) EO superlattice, (b & e) Hybrid Static superlattice, (c & f) inter-digited SL

Case 1: larger holes unbiased ( $eh1 = 2.89$ ), smaller holes biased ( $eh2 = 2.25$ )



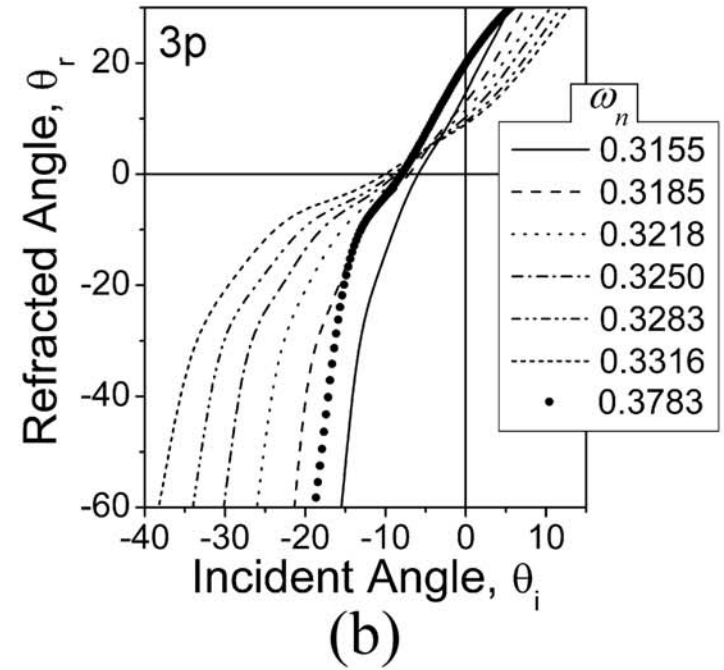
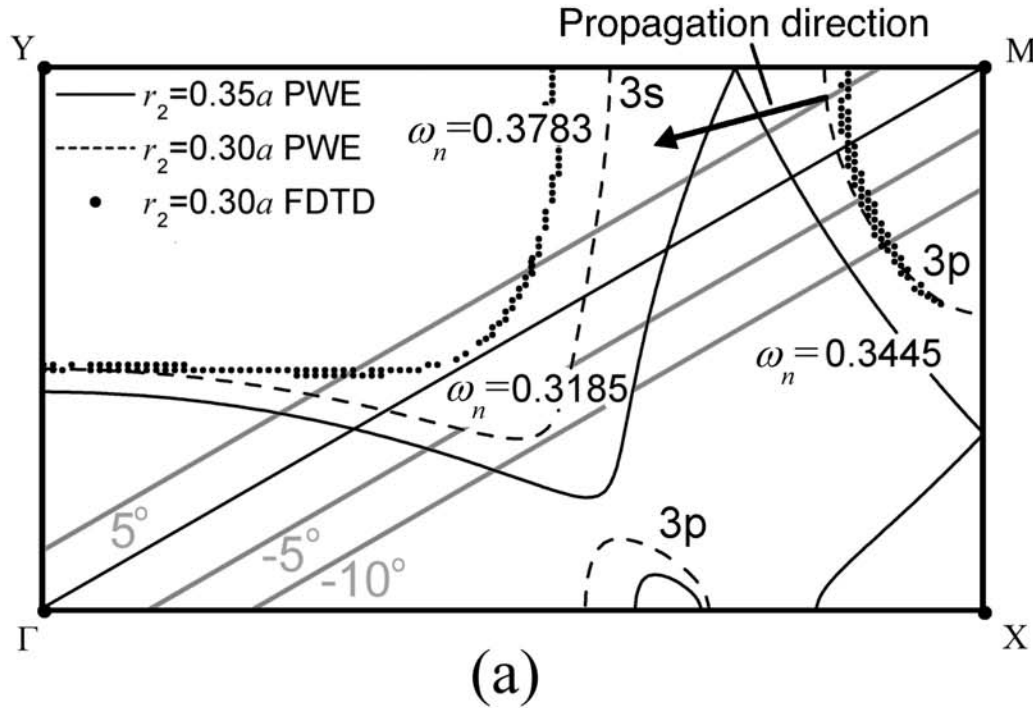
- For Hybrid Static superlattice, refraction changes from negative to positive with bias  $\Delta\theta_r = 96^\circ$  – of the order of  $80^\circ$  for other structures

# Positive & Negative Refraction

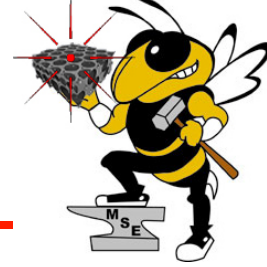


- Positive refraction  $\rightarrow$  'Snell's law' like refraction, *i.e.*  $n$  is positive
- Negative refraction  $\rightarrow n$  is negative in Snell's law
- Square and Triangular PCs  $\rightarrow$  only negative OR only positive at a fixed frequency
- SL PC  $\rightarrow$  Both regimes at a fixed frequency

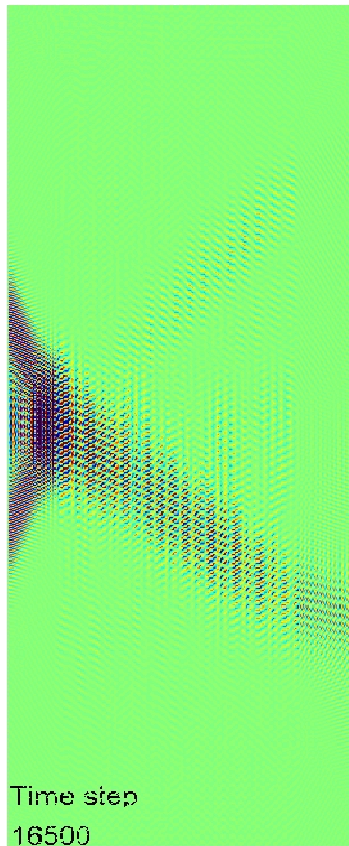
# Dispersion Contours for SSL-Structures & Spectral Dispersion Properties



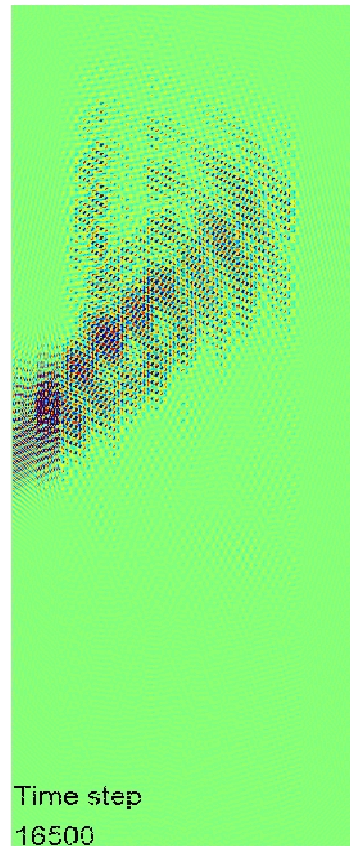
- TE polarization dispersion contours for SSL structure calculated with PWE method
  - SL strength of 1.0 (solid line) and 0.857 (dashed line)
- FDTD method for SL strength of 0.857 (scattered dots),
- Gray lines show construction lines for a beam of  $w_n = 0.3185$  incident from air
- Spectral Dispersion for  $r_2/r_1 = 0.857$  for range of  $w_n$  with 1% spacing between frequencies (group of lines) 2D slab waveguide structure (scattered plot)



- Investigation of effect coherence on refraction



$\theta_i = 0^\circ$

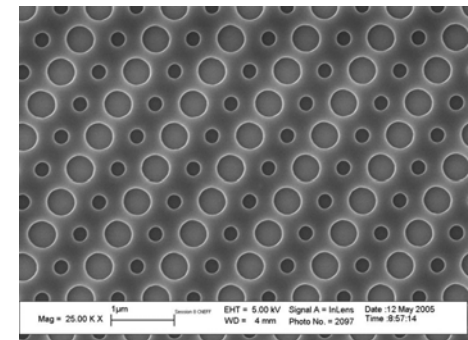


$\theta_i = 12^\circ$

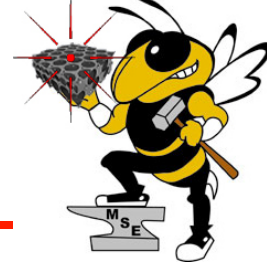
Normalized frequency = 0.309

## Static superlattice structure

- Static SL PC surrounded by silicon
- Gaussian beam: launched at incident angles of 0 and 12°. Width 24a.
- Beam steering:
  - 40.5° for  $\theta_i = 0$
  - 47.15° for  $\theta_i = 12^\circ$
- SL parameters  $r_1 = 0.35a$  and  $r_2 = 0.3a$
- SL strength:  $r_2/r_1 = 0.875$





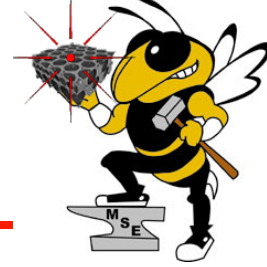


- **Control Over Dispersion Surface**
  - **Low Divergence “virtual waveguides”**
    - Beam divergence reduced by factor of  $\sim 10$
    - Optical interconnects
    - Sensor Technologies
  - **Fabry-Perot Interferometer**
    - Suitable for wavelength selection, beam width control
    - Chemical and Biological Sensing
  - **Negative Index Structures**
    - Pendry lens: Refractive Index of  $-1$

# 2D Superlattice Structures



- **Successfully developed new concept of SL PC**
  - Experimentally observed ‘band folding’ effect
- **Demonstrated that SL significantly enhances tunability, by order of magnitude, for refraction & dispersion**
- **SL introduces unique optical properties and new regimes for beam propagation effects**
  - $\Delta r$  or  $\Delta n$  between adjacent rows of holes creates a SL photonic crystal- Greater sensitivity to  $\Delta n$  by optimization of hole size ratio,  $r_2/r_1$
  - The superlattice lowers the symmetry of the structure causing:
    - **BZ folding: Band splitting removal of modal degeneracy**
    - **Highly curved Dispersion Contours near BZ boundaries**
    - **Positive and negative refraction**
    - **Beam steering of  $> 90$  degrees**
- **Hybrid superlattice enhances tunability of optical properties**



## Research Group

### Graduate Students

- Davy Gaillot
- Xudong Wang
- Swati Jain

### Postdoctoral Researchers

- Dr. Elton Graugnard,
- Dr. Jeff King
- Faculty & Staff of MiRC

**Collaborations with ARL: Drs. D. Morton, E. Forsythe & S. Blomquist**

**Supported by U.S. Army Research Office under contract MURI project  
DAAD19-01-1-0603**



---

**Thank You!!**