

# Photonic Crystal Superlattices in Electro-Optic Slab Waveguides

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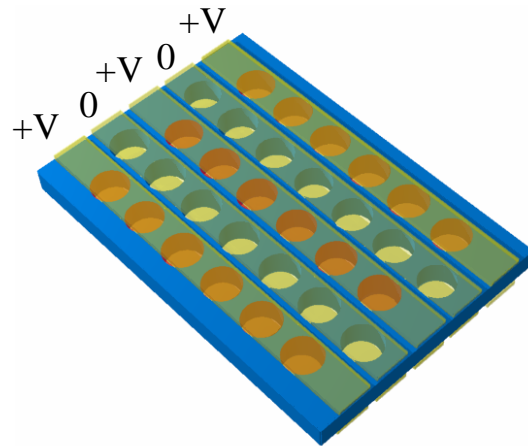


# Outline

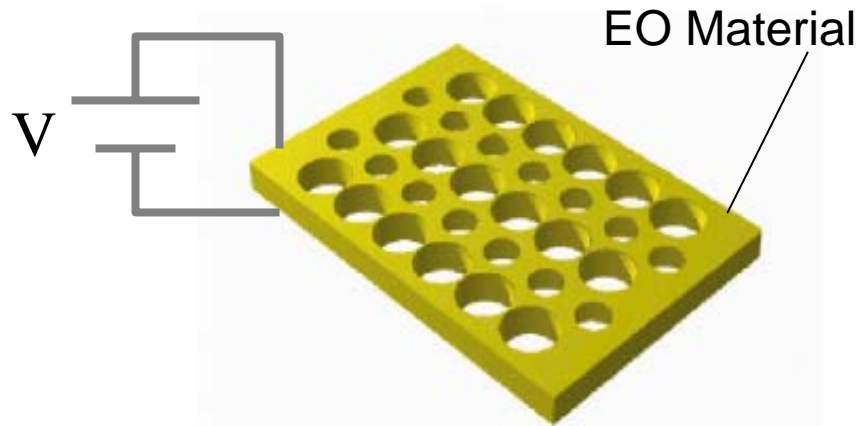


- Introduction:
  - PC superlattices
    - ‘Dynamic’
    - ‘Static’
  - Consequences of superlattice
- Details of the structure
- Results:  $\Delta r$  and bias/unbias
  - Band structure
  - Equifrequency contours
- Refraction effects
- Conclusions

# Photonic Crystal Superlattices



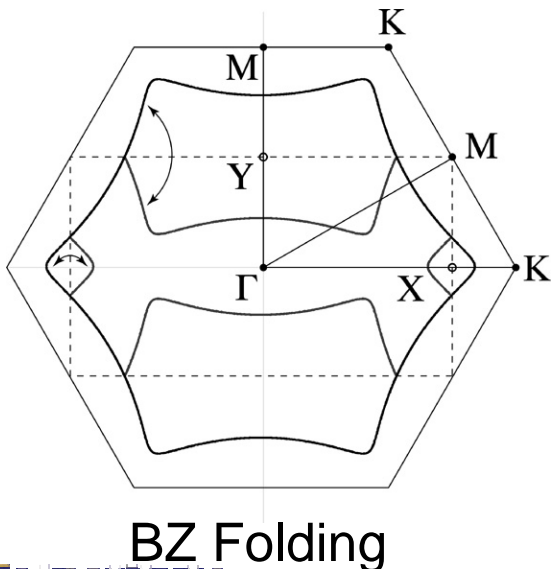
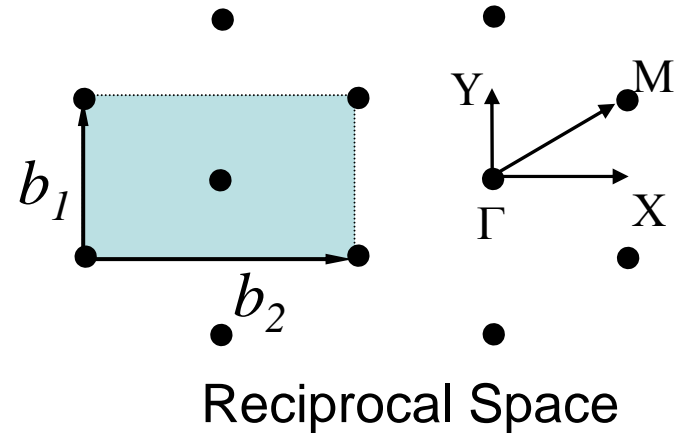
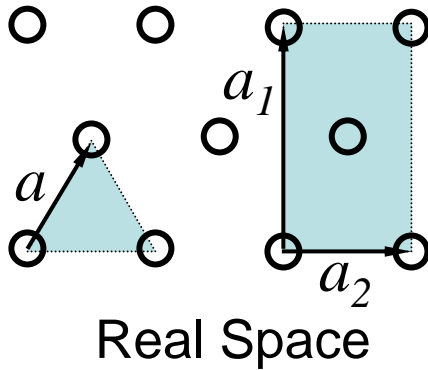
Dynamic Superlattice



'Static'/Patterned Superlattice

- Modulations in lattice between rows
  - 'Dynamic': Row addressing scheme to modulate  $n$  (Park *et al.*, *PECS IV 2002*)
  - 'Static': Modulation hardwired into device architecture
- Pattern 'static' SL in EO material to introduce tunability of optical properties

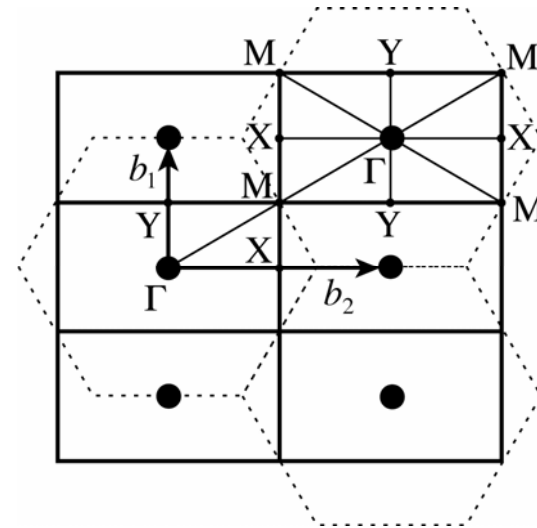
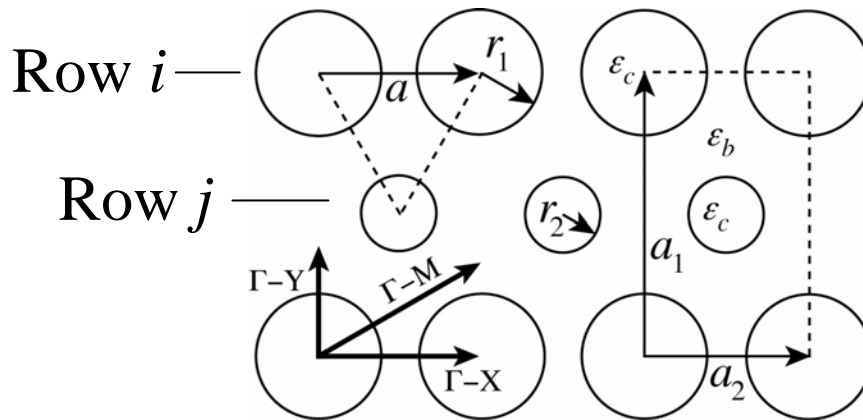
# Consequences of Superlattice



- New unit cell definition with two holes per lattice point
- New BZ representation: hexagonal becomes rectangular
- BZ folding
- Symmetry reduction



# Device Structure



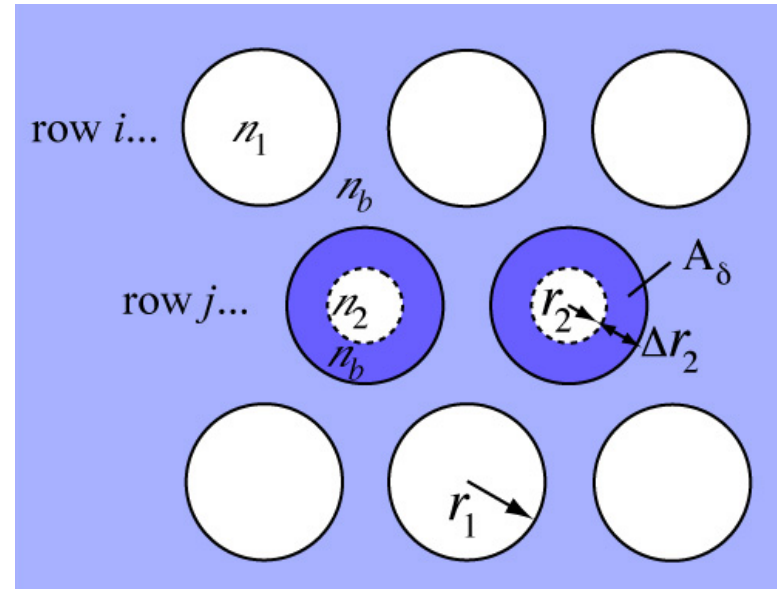
- Triangular photonic crystal patterned in EO material, i.e. PLZT, to introduce tunable properties. (Scrymgeour *et al.* *APL*, 2003, Xiong *et al.* *JQE* 2002)
- A different idea: Pattern a static superlattice into PLZT
- Row  $i$ , row  $j$  holes have radius  $r_1$ ,  $r_2$  respectively
- $r_1$  held constant while  $r_2$  decreased
- Superlattice ‘strength’ increases as ratio  $r_2/r_1$  decreases



# Superlattice Strength: Effective Index of Row $j$ Holes



- Consider index of hole weighted by the area of the hole
- Average amount of material added to structure by reducing  $r_2$  hole over the area of  $r_1$  hole
- Result is the 'effective index' of the hole
- Quantitative value of superlattice strength for comparison with dynamic superlattice
- For  $r_2/r_1=0.857$ ,  $n_{eff}=1.395$  which is  $\Delta n=0.395$  between rows of holes



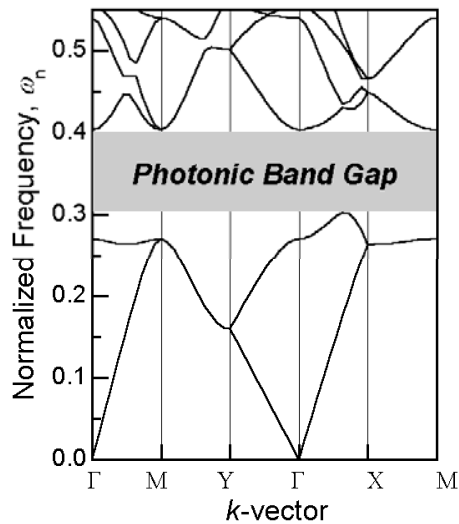
$$n_{eff} = \frac{n_b A_\delta + n_2 A_2}{A_1}$$
$$= n_b \left( 1 - \left( \frac{r_2}{r_1} \right)^2 \right) + n_2 \left( \frac{r_2}{r_1} \right)^2$$



# Band Structure: $\Delta r$ Effects

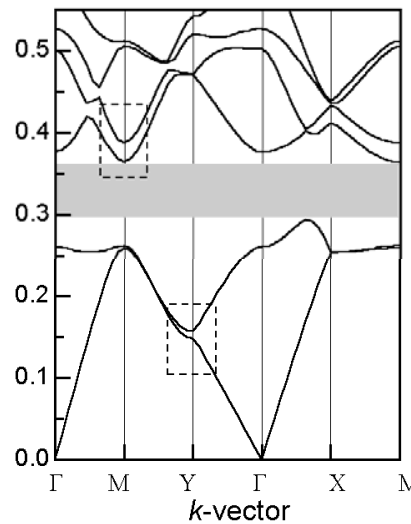


TE polarization  $r_2/r_1=1$



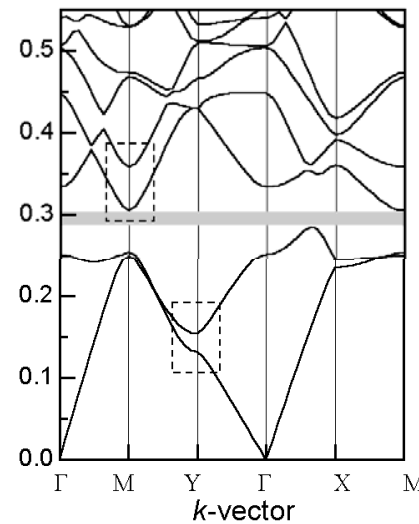
(a)

$r_2/r_1=0.857$



(b)

$r_2/r_1=0.571$



(c)

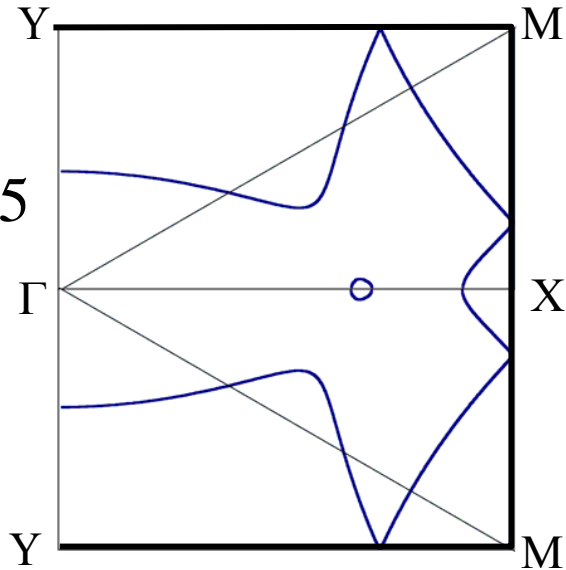
- Decreasing  $r_2$  increases amount of material in structure
- Stronger effect on air bands than dielectric bands
- Shifts bands to lower frequencies
- Decreases width of PBG
- Increases band splitting at high symmetry points



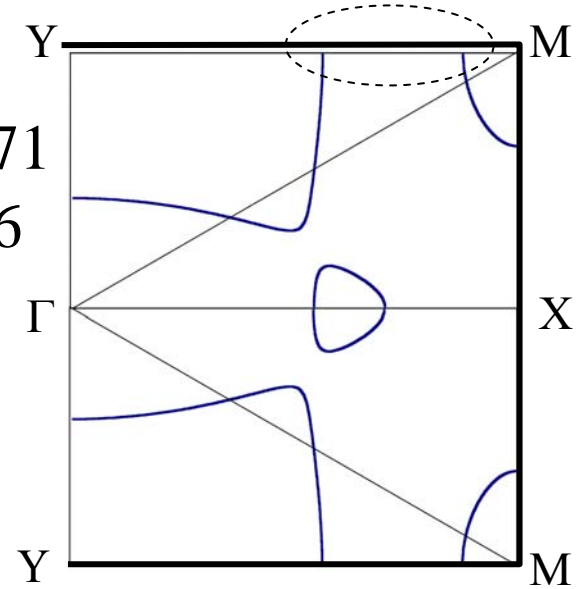
# Equipifrequency Contours: $\Delta r$



$r_2/r_1=1.0$   
 $\omega_n=0.435$



$r_2/r_1=0.571$   
 $\omega_n=0.366$



- For no radius difference, BZ folding scheme is straight forward and curves converge to a single point at BZ boundaries.
- Radius modulation causes curves to diverge/repel at BZ boundaries -- 'MQW effect'.
- Net result: relatively flat curvature in center of BZ with high curvature near BZ boundaries

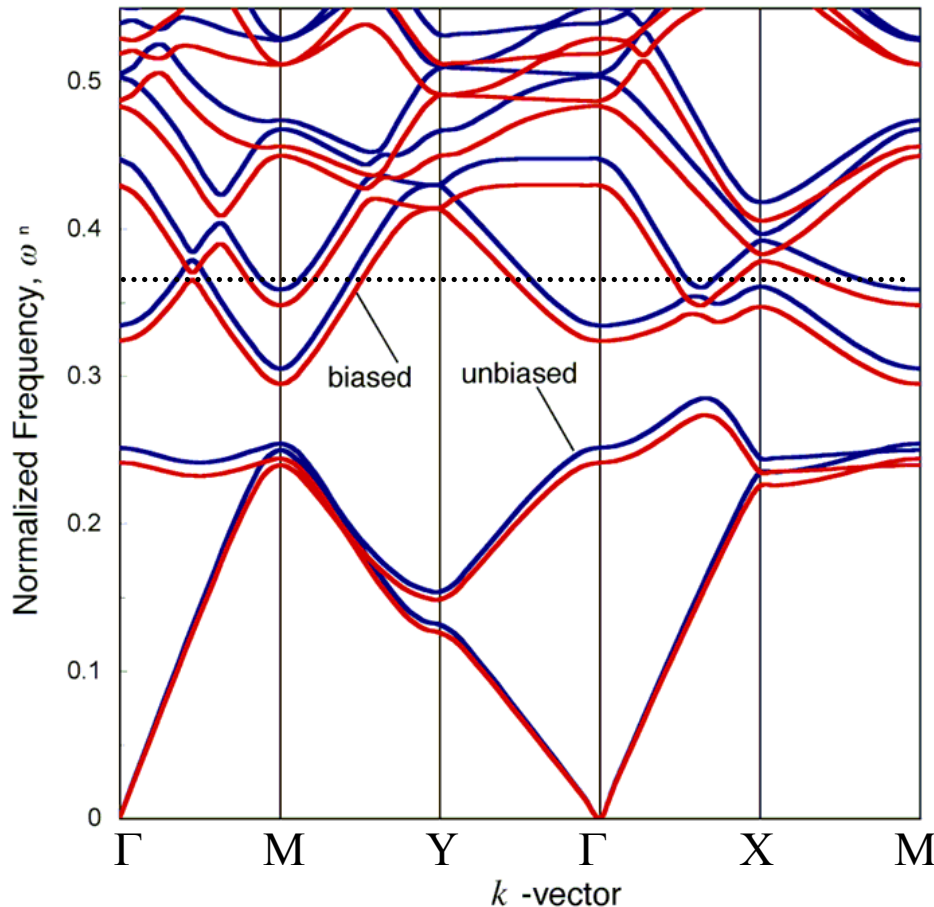




# Band Structure: Bias Effects



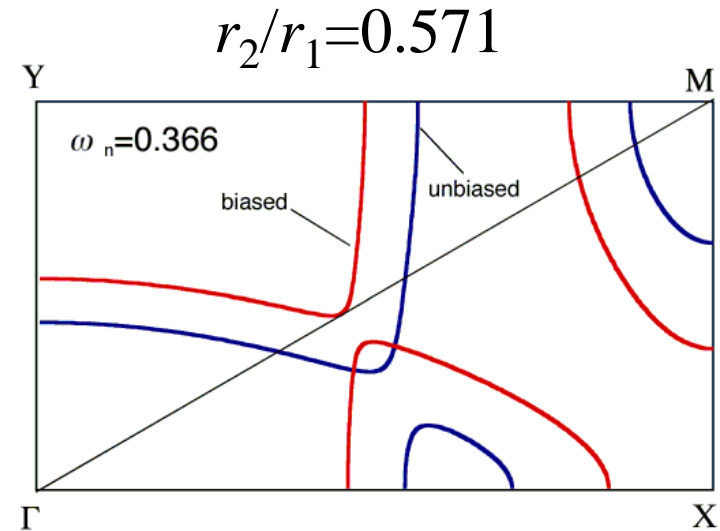
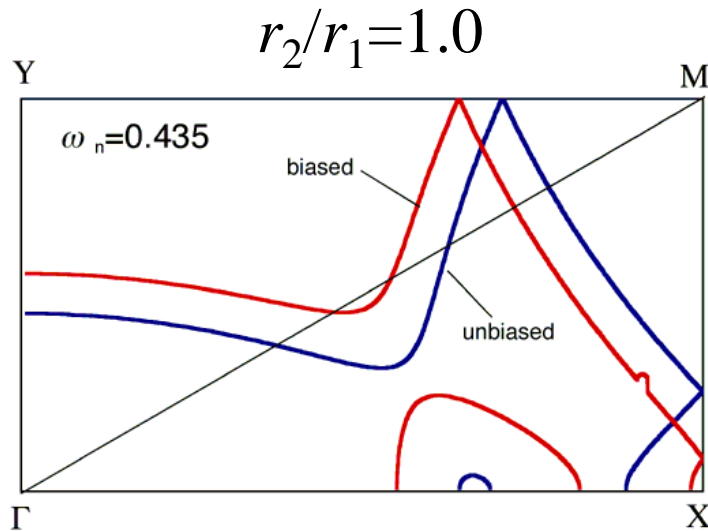
$$r_2/r_1=0.571$$



- Bias of  $6 \text{ V}/\mu\text{m}$
- Increase  $n$  from 2.49 to 2.598 ( $\Delta n \sim 0.11$ )
- Moves bands to lower frequencies
- Equifrequency line intersects bands at different points
- Dispersion surface 'looks' different for unbiased/biased cases



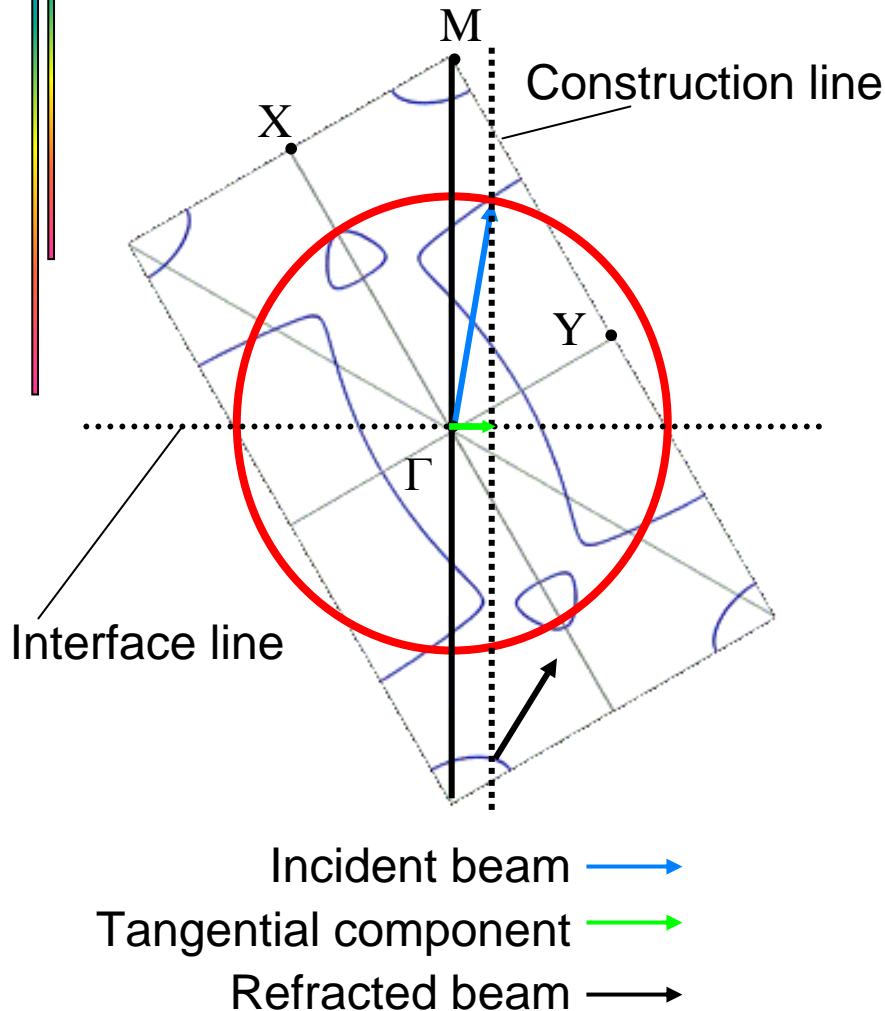
# Equipfrequency Contours: Bias Effects



- Equipfrequency plane is sectioning two different areas of the dispersion surface
- The different areas have similar contours, but they are shifted.
- Different contours results in different optical responses
  - Refraction/Beam steering
  - Switching/Modulation
  - Dispersion



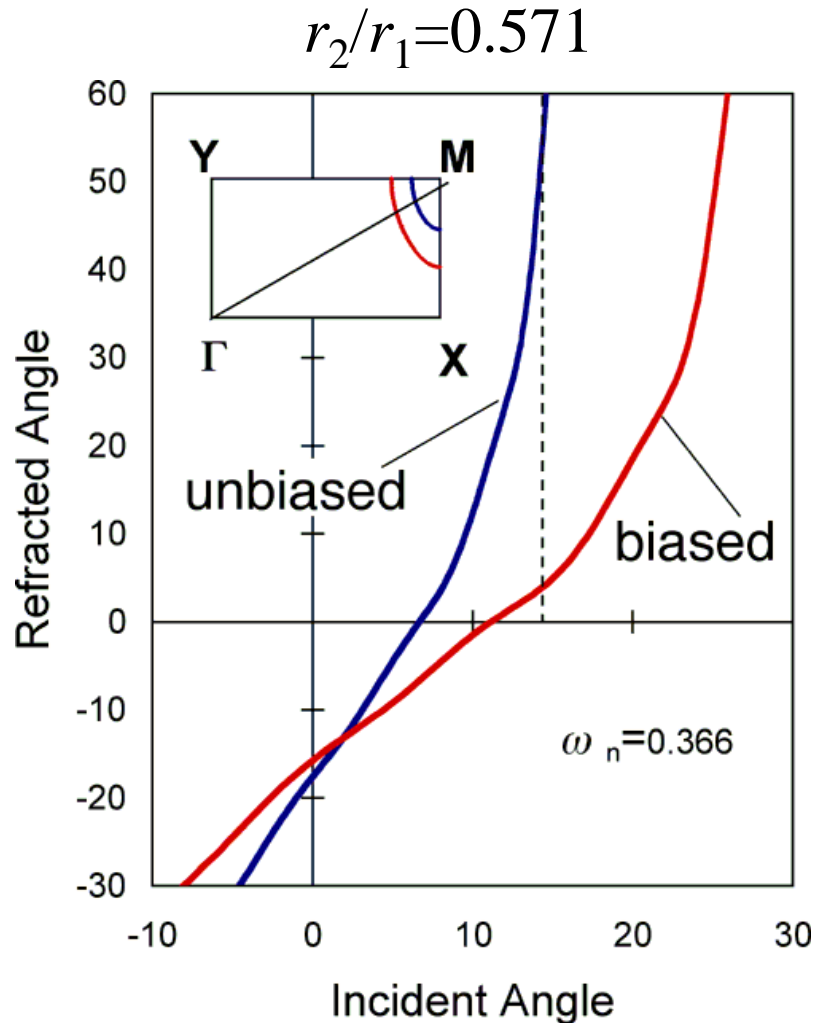
# $k$ -vector Diagrams



- Outlined by Russell *et al.* 1996 and Kosaka *et al.* *PRB* 1998
- Analysis done in  $k$ -space
- Tangential component of incident beam conserved at interface
- Conservation condition satisfied at intersection of construction line with EFC
- Refraction angle determined by curvature of EFC
- Final direction of Poynting vector is normal to EFC at point of intersection



# Refraction Results



- Bias changes  $n$  which shifts the EFCs
- At  $\sim 14^\circ$  incident angle,  $\sim 55^\circ$  change in refraction angle
- Increase in effect over triangular lattice
- Refraction occurs at zero incident angle
- Two regimes of refraction: negative and positive



# Conclusion

- A modulation in hole radii between adjacent rows of holes creates a superlattice.
- The superlattice lowers the symmetry of the structure causing:
  - BZ folding
  - Band splitting at BZ boundaries
  - Highly curved EFCs near BZ boundaries
- Tunability of refraction  $>55^\circ$  with  $\Delta n \sim 0.11$
- Greater sensitivity to  $\Delta n$  can be possible through optimization of hole size ratio,  $r_2/r_1$



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